

LECTURE NOTES
ON
HYDRAULIC MACHINE & IFP



5th SEMESTER

PREPARED BY

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BRANCH:- MECHANICAL ENGG.

SUBJECT:- HYDRAULIC MACHINE & I/P

SEMESTER:- 5th SEM (DIPLOMA)

HM & IFD

(1) Turbine :-

- (i) pelton wheel Turbine.
- (ii) Francis Turbine.
- (iii) Kaplan Turbine.

(2) Pump :-

- (i) Centrifugal pump.
- (ii) Reciprocating pump.

(3) IFC :-

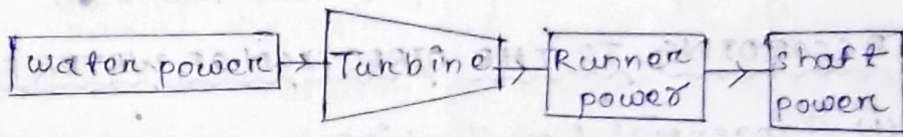
- (i) Pneumatic Control system.
- (ii) Hydraulic control system.

HYDRAULIC MACHINE:-

Those machines which are runs with the help of water are called hydraulic machine.

Ex:- Turbine, pump.

TURBINE:- Turbine is a hydraulic machine which converts water power to mechanical power / shaft power is known as turbine.

CLASSIFICATION OF TURBINE:-(1) ACCORDING TO THE ENERGY AT INLET:-

- (i) Impulse turbine.
- (ii) Reaction turbine.

(i) IMPULSE TURBINE:-

If at the inlet of the turbine the energy available is only kinetic energy then it is called impulse turbine. Ex:- (Pelton turbine).

(ii) REACTION TURBINE:-

If at the inlet the water possess kinetic energy as well as pressure energy is called Reaction Turbine. Ex:- (Francis Turbine).

(2) ACCORDING TO THE HEAD OF WATER?

- (i) Low head of water turbine (0-5 m)
- (ii) Medium head of water turbine (5-25 m)
- (iii) High head of water turbine (25 - Above)

(3) ACCORDING TO THE SPECIFIC SPEED?

- (i) Low specific speed (> 25 rpm).
- (ii) Medium specific speed (25-250 rpm).
- (iii) High specific speed (More than 250)

(4) ACCORDING TO THE DIRECTION OF WATER FLOW?

- (i) Tangential flow Turbine.
- (ii) Radial flow Turbine.
- (iii) Axial flow Turbine.
- (iv) Mixed flow Turbine.

(i) TANGENTIAL FLOW TURBINE?

If the water flows along tangent of the runner then turbine is called tangential flow turbine. Ex:-(Pelton wheel turbine).

(ii) RADIAL FLOW TURBINE?

If the water flow in the radial direction through the runner is called Radial flow turbine. Ex:-(Francis turbine).

Types:- (1) Outward radial flow.
(2) Inward radial flow.

(1) Outward radial flow?

If water flows inward to outward radially then it is called outward radial flow turbine.

(2) Inward radial flow Turbine:-

If water flow outward to inward radially then turbine is called inward radial flow turbine.

(iii) AXIAL FLOW:-

If water flows parallel to the axis of the rotation of the runner then it is called axial flow turbine. EX:- (Kaplan turbine).

(iv) MIXED FLOW TURBINE:-

If the water flows through the runner in radial direction but leaves parallel to the axis of the rotation of runner is called mixed flow turbine. (Axial + Radial flow turbine).

EFFICIENCIES OF A TURBINE:-

(1) Hydraulic efficiency:-

It is defined as the ratio between power given by water to the runner of a turbine to the power supplied by the water at the inlet of turbine.

$$\eta_H = \frac{\text{Runner power}}{\text{water power}}$$

$$\text{water power} = \frac{\rho \times g \times Q \times H}{1000} \text{ Kw.}$$

(2) Mechanical efficiency:-

The power delivered by water to the runner of a turbine is transmitted to the shaft of the turbine.

$$\eta_m = \frac{\text{Power at the shaft}}{\text{Runner power.}}$$

$$\therefore \text{Shaft power} = \frac{2\pi NT}{60 \times 10^3} \text{ Kw.}$$

(3) Overall efficiency:-

$$\eta_o = \eta_m \times \eta_H$$

$$\eta_o = \frac{S.P.}{R.P.} \times \frac{R.P.}{W.P.} = \frac{S.P.}{W.P.}$$

* So It is the ratio between shaft power to water power.

(4) Volumetric efficiency:-

The volume of the water striking the runner of a turbine is slightly less than volume of water supplied to the turbine.

$$\eta_{vol} = \frac{\text{Volume of water actually striking runner}}{\text{Volume of water supplied to the turbine.}}$$

SOLVED PROBLEMS:-

(Q) In a hydraulic turbine, the mechanical and hydraulic efficiencies are 83% and 89%. Find the overall efficiency?

Ans:- Given Data

$$\eta_m = 83\% = 0.83$$

$$\eta_H = 89\% = 0.89$$

we know that overall efficiency

$$\eta_o = \eta_H \times \eta_m$$

$$\eta_o = 0.83 \times 0.89 = 0.7387$$

$$= 73.87\%$$

Ans

(Q) Find out the overall efficiency of a hydraulic turbine where the shaft power is 860 kW and the turbine runs under a head of 15 meters and the discharge is $2000 \text{ m}^3/\text{sec}$?

Ans:-

$$S.P = 860 \text{ kW}$$

$$Q = 2000 \text{ m}^3/\text{sec}$$

$$h = 15 \text{ meter}$$

We know that

$$\text{water power} = \rho \times g \times Q \times h$$

$$w.p = 1000 \times 9.81 \times 2000 \times 15$$

$$= 294300000 \div 1000$$

$$= 294300 \text{ kW}$$

\therefore overall efficiency.

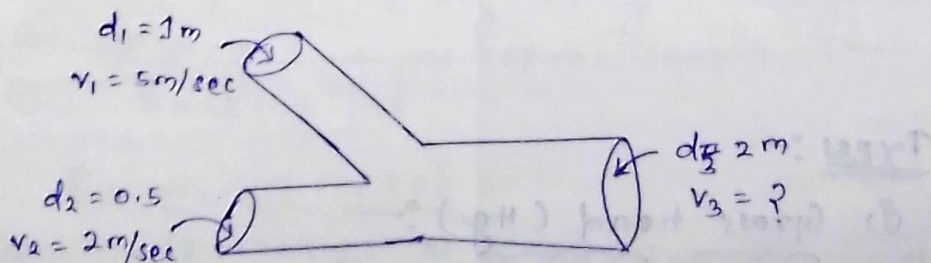
$$\eta_o = \frac{S.P}{w.p} = \frac{860}{294300}$$

$$= 0.00292218824$$

$$= 0.292218824 \%$$

Ans

(Q) In a pipe line which is described as below



Find the value of v_3 ?

Ans:- Given Data.

$$d_1 = 1 \text{ m}, \quad d_2 = 0.5 \text{ m}, \quad d_3 = 2 \text{ m}$$

$$v_1 = 5 \text{ m/sec}, \quad v_2 = 2 \text{ m/sec}, \quad v_3 = ?$$

We know that

Applying continuity equation in this equation.

$$Q_1 + Q_2 = Q_3$$

$$A_1 V_1 + A_2 V_2 = A_3 V_3$$

$$Q_1 = \frac{\pi}{4} \times (1)^2 \times 5 = 3.9 \text{ m}^3/\text{sec} \quad A_3 = \frac{\pi}{4} \times 2^2 = 3.14$$

$$Q_2 = \frac{\pi}{4} \times (0.5)^2 \times 2 = 0.38 \text{ m}^3/\text{sec}$$

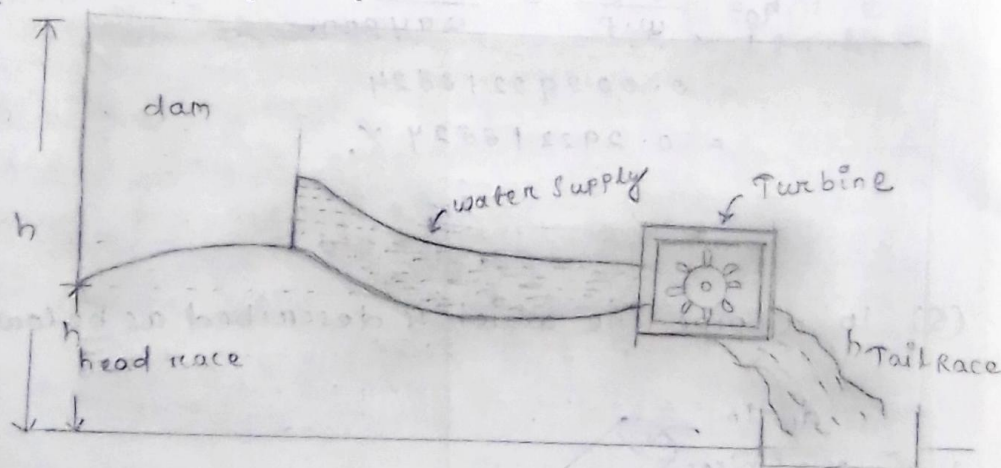
$$Q_3 = 3.9 + 0.38 = 3.14 \times V_3$$

$$\Rightarrow 4.28 = 3.14 \times V_3$$

$$\Rightarrow V_3 = \frac{4.28}{3.14} = 1.36 \text{ m/sec}$$

Ans

HEAD USED IN TURBINE:-



Types:-

(i) Gross head (H_g):-

→ head race - h tail race

(ii) Net head:-

→ (H_g - H_f)

where, H_f = head loss due to friction

H_g = Gross head.

PELTON WHEEL TURBINE

It is a purely impulse turbine that means the energy available at inlet is kinetic energy. It works on high head of water. It has low discharge & low specific speed.

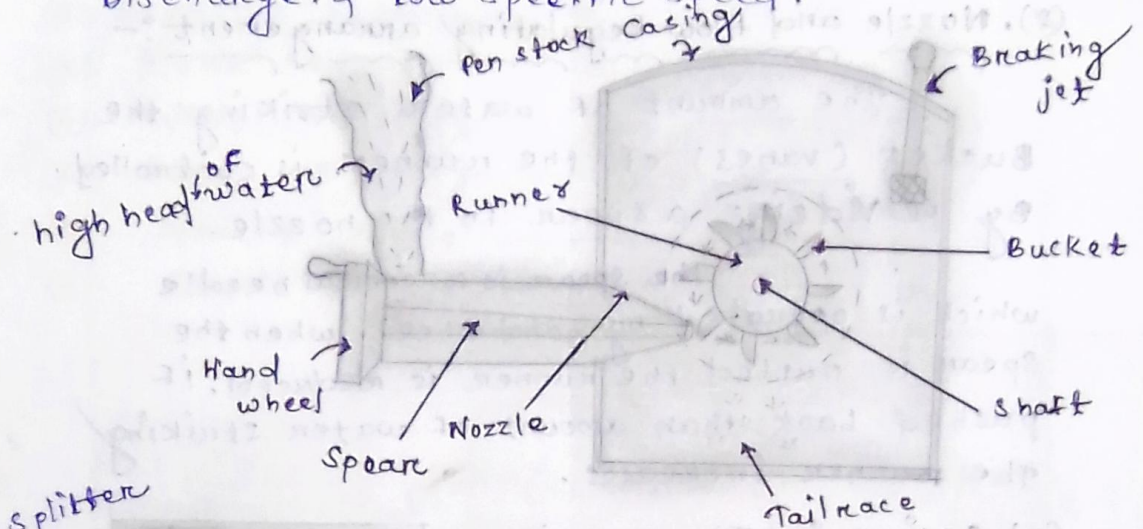


Fig:- Pelton wheel turbine.

Fig:- Bucket - (Double hemi-spherical shape).

IMPORTANT PARTS OF PELTON WHEEL TURBINE

- (1). Runner and Bucket.
- (2). Nozzle and flow regulating Arrangement.
- (3). Casing (To protect accidents)
- (4). Braking jet.

(1). Runner and Bucket :-

It consist of a circular disc on the periphery with a number of buckets evenly spaced are fixed the shape of bucket is Double hemi spherical cup. each bucket is divided into two symmetrical parts by a dividing wall called splitter.

The jet of water strikes the splitter which divided the jet into two equal part. the Bucket are so shaped that the jets get Deflected at an angle of 160° to 170° .

(2). Nozzle and Flow Regulating arrangement :-

The amount of water striking the Bucket (vanes) of the runner is controlled By providing a spear in the nozzle.

The spear is a conical needle which is operated by hand wheel. when the spear is pushed the runner is reduced, if pushed back than amount of water striking the runner increases.

(3) Casing :- The function of the casing is to prevent the splashing of water and to discharge it into tail race. It acts as a safeguard Against accident. It has no hydraulic function.

(4) Braking jet :-

When the nozzle is completely closed By moving the spear in Forward direction The amount of water striking the runner Reduces to zero. But due to inertia the runner goes on revolving to stop it in less time a small nozzle is provided on the back of the vanes is known as Braking jet.

* Force exerted by the water

$$f = m \times a$$

$$f = m \times \frac{dv}{dt} \quad \left[a = \frac{dv}{dt} \text{ (the rate of change of velocity)} \right]$$

$$f = \frac{d}{dt} \cdot m \times v \quad \left[\text{Momentum} = \frac{d}{dt} \right]$$

$$= m \times \frac{d}{dt} (v)$$

$$= m \times (\text{initial velocity} - \text{final velocity})$$

[m - mass flow rate]

Applying continuity equation

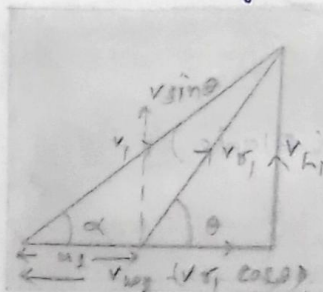
$$A_1 v_1 = A_2 v_2 \quad (\text{when the } \rho = c)$$

$$\rho_1 A_1 v_1 = \rho_2 A_2 v_2 \quad (\text{when the } \rho \neq c)$$

$$= \rho \times a \times v_{r1} (v_{r1} - v_{r2}) \quad \left\{ \begin{array}{l} \text{In more than one velocity} \\ \text{we can take relative} \\ \text{velocity.} \end{array} \right.$$

$$(i) -v_{r1} \cos \theta = v_{w1} - u_1$$

$$(ii) -v_{r2} \cos \phi = v_{w2} - u_2$$



$$f = \rho \times a \times v_{r1} (v_{r1} - v_{r2}) \quad \left[\begin{array}{l} \text{[-ve sign due to opposite} \\ \text{directions]} \\ \text{(equation is take +ve)} \end{array} \right] \quad \left(u_1 = u_2 \right)$$

$$= \rho \times a \times v_{r1} (v_{w1} \pm v_{w2})$$

$$f = \rho \times a \times v_{r1} (v_{w1} \pm v_{w2})$$

$$\therefore \text{Runner power} = f \times v = \frac{\rho \times a \times v_{r1} (v_{w1} \pm v_{w2}) \times u}{1000} \text{ kW}$$

where,

ρ = density

a = area of the jet $\left[a = \frac{\pi}{4} \times d^2 \right]$

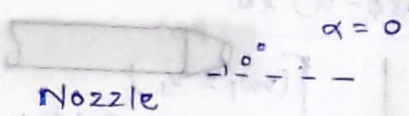
v_{r1} = Relative velocity

v_{w1} = whirl velocity

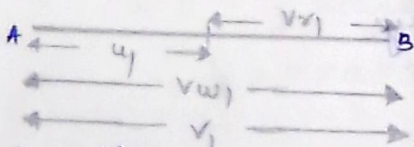
u = Blade velocity.

PELTON WHEEL TURBINE (RUNNER POWER)

→ In a pelton wheel turbine α angle is zero.



→ When the $\alpha = 0^\circ$ the the inlet velocity Diagram is below:-



Equations are in create:-

$$(1) v_{r1} = v_{w1} - u_1$$

$$(2) v_{w1} = v_1$$

$$(3) u_1 = v_{w1} - v_{r1}$$

$$(4) u_1 = v_1 - v_{r1}$$

$$(5) v_{r1} = v_1 = u_1$$

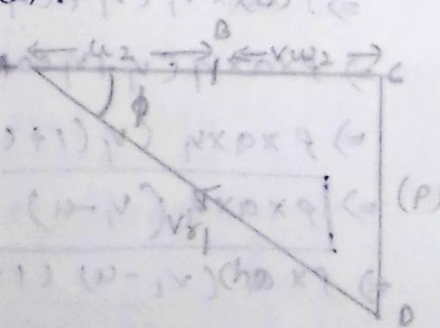
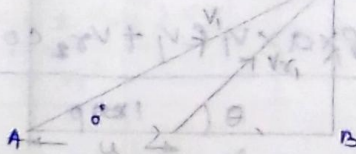
→ out let velocity diagram:-

$$\cos \phi = \frac{b}{h_1}$$

$$\cos \phi = \frac{u_2 - v_{w2}}{v_{r2}}$$

$$\Rightarrow v_{r2} \cos \phi = u_2 + v_{w2}$$

$$\Rightarrow v_{w2} = v_{r2} \cos \phi - u_2$$



→ We know the the runner power of pelton wheel turbine is

$$R.P = \frac{\rho \times a \times v_{r1} (v_{w1} + v_{w2}) \times u}{1000} \text{ kW}$$

∴ To putting the value of v_{r1} & v_{w1}, v_{w2} Then R.P is

$$R.P = \frac{\rho \times a \times v_1 (v_1 + v_{r2} \cos \phi - u) \times u}{1000} \text{ kW}$$

where,

ρ = Density

a = area of the jet

v_{r1} = Relative velocity

v_{w1} = wheel velocity

u = Blade velocity

v_1 = Absolute velocity

α = Nozzle angle

θ = Blade angle

$$\begin{cases} (v_{w1} = v_1) \\ v_{w2} = v_{r2} \cos \phi - u \\ u = u_2 \end{cases}$$

* When the change its triangle to a line then we take Absolute velocity, then R.P is

$$R.P = \frac{\rho \times a \times v_1 (v_1 + v_{r2} \cos \phi - u) \times u}{1000} \text{ kW}$$

$$\begin{cases} v_{r1} = v_{r2} \end{cases}$$

To simplify it

$$R.P = \rho \times a \times v_1 (v_1 + v_{r1} \cos \phi - u) \times u$$

$$\Rightarrow \rho \times a \times v_1 (v_1 + (v_1 - u) \cos \phi - u) \times u$$

$$\Rightarrow \rho \times a \times v_1 (v_1 + v_1 \cos \phi - u \cos \phi - u) \times u$$

$$\Rightarrow \rho \times a \times v_1 (v_1 (1 + \cos \phi) - u (1 + \cos \phi)) \times u$$

$$\Rightarrow \boxed{\rho \times a \times v_1 (v_1 - u) (1 + \cos \phi) \times u}$$

$$\Rightarrow \rho \times a \times (v_1 - u) (1 + \cos \phi) \times u$$

$$\begin{cases} v_{r1} = v_1 - u \\ \phi = \alpha \times v \end{cases}$$

HYDRAULIC EFFICIENCY OF PELTON WHEEL TURBINE:

1) $\eta_H = \frac{R.P}{W.P}$ where, R.P = Runner Power
W.P = Water Power

$$= \frac{\rho \times a \times v_1 (v_{w1} \pm v_{w2}) \times u}{\rho \times g \times a \times H}$$

$$= \frac{\rho \times a (v_{w1} \pm v_{w2}) \times u}{\rho \times g \times a \times H} \quad [a \times v_1 = Q]$$

$$\Rightarrow \eta_H = \frac{(v_{w1} \pm v_{w2}) \times u}{g \times H}$$

(2) if we consider the kinetic energy of water

$$K.E = \frac{1}{2} \times m \times v_1^2$$

$$= \frac{1}{2} \times \rho \times a \times v_1 \times v_1^2 \quad \left[\begin{array}{l} m = \rho a v = \text{constant} \\ \text{Liquid mass flow rate} \end{array} \right]$$

$$\eta_H = \frac{R.P}{W.P} = \frac{\rho \times a \times v_1 (v_{w1} \pm v_{w2}) \times u}{\frac{1}{2} \times \rho \times a \times v_1 \times v_1^2}$$

$$\eta_H = \frac{2 (v_{w1} \pm v_{w2}) \times u}{v_1^2}$$

$$\Rightarrow \frac{2 (v_1 + v_{r2} \cos \phi - u) \times u}{v_1^2}$$

$$\Rightarrow \frac{2 (v_1 + v_{r1} \cos \phi - u) \times u}{v_1^2}$$

$$\Rightarrow \frac{2 (v_1 + (v_1 - u) \cos \phi - u) \times u}{v_1^2}$$

$$\Rightarrow \frac{2 (v_1 + (v_1 \cos \phi - u \cos \phi) - u) \times u}{v_1^2}$$

$$\Rightarrow \frac{2 (v_1 (1 + \cos \phi) - u (1 + \cos \phi)) \times u}{v_1^2}$$

$$\Rightarrow \eta_H = \frac{2 (v_1 - u) (1 + \cos \phi) \times u}{v_1^2}$$

$$\left[\begin{array}{l} v_{r1} = v_{r2} \\ v_{r1} = v_1 - u \end{array} \right]$$

* What is the condition for max^m efficiency of Turbine.

So let us say

To find the max^m efficiency with respect to Blade speed.

$$= \boxed{\frac{d}{du} (\eta_H) = 0}$$

$$\Rightarrow \frac{d}{du} \left[\frac{2(v_1 - u)(1 + \cos \phi) \times u}{v_1^2} \right]$$

$$\Rightarrow \frac{1 + \cos \phi}{v_1^2} \times \left(\frac{d}{du} 2(v_1 - u) \times u^2 \right)$$

$$\Rightarrow \frac{1 + \cos \phi}{v_1^2} \times 2 \times \frac{d}{du} v_1 u - \frac{d}{du} u^2$$

$$\Rightarrow \frac{1 + \cos \phi}{v_1^2} \times 2(v_1 - 2u)$$

$$\Rightarrow \frac{2(1 + \cos \phi)}{v_1^2} (v_1 - 2u) = 0$$

∴ for max^m efficiency

$$u_1 = 2u = 0$$

$$v_1 = 2u$$

$$\boxed{u = \frac{v_1}{2}}$$

$$\eta_H = \frac{2(v_1 - u)(1 + \cos \phi) \times u}{v_1^2}$$

$$= \frac{2(2u - u) \times (1 + \cos \phi) \times u}{(2u)^2}$$

$$= \frac{4u - 2(1 + \cos \phi) \times u}{4u^2}$$

$$= \boxed{\frac{2u \times u \times (1 + \cos \phi)}{4u^2}}$$

$$\left[\begin{array}{l} \frac{d}{du} v_1 u \\ v_1 \frac{d}{du} u = v_1 \end{array} \right]$$

$$\left[\begin{array}{l} \frac{d}{du} u^2 = 2u \\ \frac{d}{du} u^2 = 2u \end{array} \right]$$

$$\Rightarrow \frac{2u^2}{4u^2} \times (1 + \cos \phi)$$

$$\Rightarrow \boxed{\eta_{\max} = \frac{1 + \cos \phi}{2}}$$

$$[v_1 = 2u]$$

SOLVED PROBLEMS:-

(Q2) A pelton wheel turbine having Bucket speed of 10 m/s and water flows at the rate of 700 liters/second, under a head of 30 meters. The Bucket Deflects through an angle of 160° calculate the Runner power and hydraulic efficiency when $C_v = 0.98$.

Ans:-

Given data

$$u = 10 \text{ m/sec}$$

$$\rho = 1000 \text{ kg/m}^3$$

$$Q = 700 \text{ liter/sec} = 700 \times 10^{-3} \text{ m}^3/\text{sec}$$

$$h = 30 \text{ m}$$

$$d\theta = 160^\circ$$

$$C_v = 0.98 \text{ (coefficient of velocity)}$$

$$(1) v_1 = C_v \sqrt{2gh}$$

$$= 0.98 \sqrt{2 \times 9.81 \times 30}$$

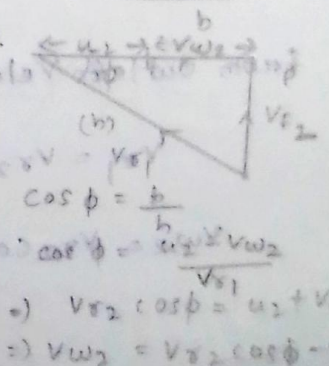
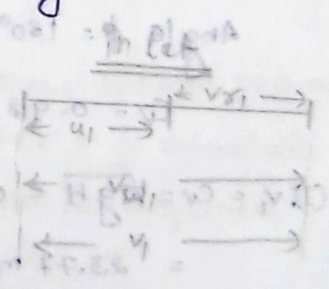
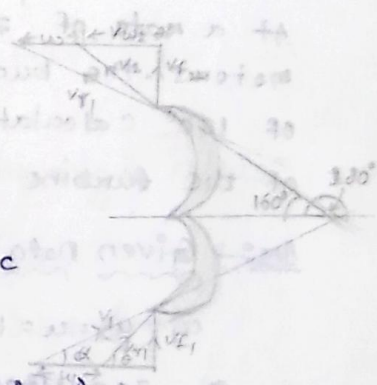
$$= 23.77 \text{ m/sec}$$

$$\therefore \phi = 180^\circ - 160^\circ = 20^\circ$$

$$R.P = \rho \times Q [(v_1 + (v_1 - u) \cos \phi - u) \times u]$$

$$\Rightarrow 1000 \times 700 \times 10^{-3} (23.77 + (23.77 - 10) \times \cos 20^\circ - 10) \times 10$$

$$\Rightarrow 1000 \times 700 \times 10^{-3} (23.77 + (23.77 \cos 20^\circ - 10) \times 10)$$



$$(2) \eta_H = \frac{R.P.}{W.P.} = \frac{1000 \times 700 (23.77 + 23.77 \cos 20^\circ - 10) \times 10}{\rho \times g \times Q \times H}$$

$$\Rightarrow \frac{1000 \times 700 (23.77 + 23.77 \cos 20^\circ - 10) \times 10}{1000 \times 9.81 \times 700 \times 30}$$

$$\Rightarrow \frac{23.77 + 23.77 \cos 20^\circ - (0) \times 10}{9.81 \times 30}$$

$$\Rightarrow 0.87 \approx 87\%$$

Ans

(Q2) A Pelton wheel turbine has a mean bucket speed of 10 meter per second with a jet of water flowing at a rate of 700 liter/second under a head of 30 meters. The bucket deflect the jet through an angle of 160° calculate the runner power, hydraulic efficiency of the turbine. Assume $C_v = 0.98$,

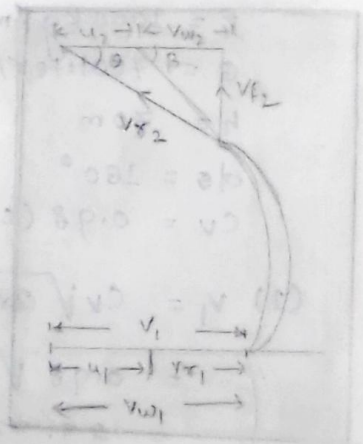
Ans - Given Data

$$u_1 = u_2 = u = 10 \text{ m/s} \quad H = 30 \text{ m}$$

$$Q = 700 \text{ liter/sec}$$

$$\text{Angle } \phi = 180^\circ - 160^\circ = 20^\circ$$

$$C_v = 0.98$$



$$(1) v_1 = C_v \sqrt{2gH} = 0.98 \sqrt{2 \times 9.81 \times 30}$$

$$= 23.77 \text{ m/s}$$

$$v_{w1} = v_1 = 23.77 \text{ m/s}, \quad v_{r1} = v_1 - u_1 = 23.77 - 10 = 13.77 \text{ m/s}$$

from outlet velocity triangle

$$v_{r1} = v_{r2} = 13.77 \text{ m/s}$$

$$v_{w2} = v_{r2} \cos \phi - u_2 = 13.77 \cos 20^\circ - 10 = 2.94 \text{ m/s}$$

$$\begin{aligned}
 (2) \text{work done} &= \rho \times a \times v_1 [v_{w1} + v_{w2}] \times u \\
 &= 1000 \times 0.7 [23.77 + 2.94] \times 10 \\
 &= 186970 \text{ N/m}^2 = 186.97 \text{ kW}
 \end{aligned}$$

$$(3). \eta_H = \frac{2 [v_{w1} + v_{w2}] \times u}{v_1^2} = \frac{2 [23.77 + 2.94] \times 10}{(23.77)^2} = 99\%$$

Ans

POINTS TO BE REMEMBERED FOR PELTON WHEEL TURBINE

(1). The velocity of jet at inlet $v_1 = \sqrt{2gH}$

C_v = Co-efficient of velocity (0.98 to 0.99)

(2). Velocity wheel (u) = $\phi \sqrt{2gH}$

$\frac{u}{v_1}$ ← ϕ = speed ratio (0.43 to 0.98)

(3). If no angle is given then jet deflection angle is 165°

(4). Jet ratio (d) = $\frac{f}{d} = \frac{\text{Pitch diameter}}{\text{Jet diameter}}$

(5). No. of Buckets on the Runner (Z) = $15 + \frac{D}{2d}$

(Q3) A pelton wheel turbine is designed for the following specification:

Shaft power = 11,722 kW, Head = 380 m, Speed = 750 rpm

Overall efficiency = 86%, Jet diameter = $\frac{1}{6}$ wheel dia.

Determine (1) wheel diameter (2) No. of jet required.

(3) Diameter of jet

Ans:-

Given Data:-

S.P = 11,722 kW, $N = 750 \text{ rpm}$.

$H = 380 \text{ m}$, $\eta_o = 0.86$.

$d = \frac{1}{6} D$, $C_v = 0.985$

$$\Rightarrow \frac{d}{D} = \frac{1}{6}$$

We know that

$$(1) v_1 = C_v \sqrt{2gH} = 0.98 \sqrt{2 \times 9.81 \times 380} = 85.05 \text{ m/s}$$

$$(2) u_1 = u_2 = u = \phi \times \sqrt{2gH} = 0.45 \sqrt{2 \times 9.81 \times 380}$$

$$= 38.85 \text{ m/s}$$

$$(3) u = \frac{\pi D N}{60} \Rightarrow D = \frac{60 \times u}{\pi \times N} = \frac{60 \times 38.85}{3.14 \times 750} = 0.989 \text{ m}$$

$$(4) d = \frac{1}{6} D = \frac{0.989}{6} = 0.165 \text{ m}$$

(5) Discharge from one jet (Q) = A x v

$$\Rightarrow \frac{\pi}{4} \times d^2 \times v_1 = \frac{\pi}{4} \times (0.165)^2 \times 85.05 = 1.818 \text{ m}^3/\text{s}$$

(6) Overall efficiency $\eta_o = \frac{S.P.}{W.P.}$

$$\Rightarrow 0.86 = \frac{11,722}{W.P.}$$

$$\Rightarrow W.P. = \frac{11,722}{0.86}$$

$$\Rightarrow \frac{\rho \times g \times Q \times H}{1000} = \frac{11,722}{0.86}$$

$$(Q) \Rightarrow 3.672 \text{ m}^3/\text{s}$$

(7) No. of jet required = $\frac{Q}{q} = \frac{3.672}{1.818} = 2 \text{ jet}$

REACTION TURBINES

At the inlet there is kinetic energy as well as pressure energy of water is used.

EX: Francis turbine.

$$K.E = \frac{1}{2} \times m \times v^2$$

$$P.E = \rho \times g \times H$$

FRANCIS TURBINE:-

It is a Inward flow reaction turbine having radial discharge at outlet. In modern Francis turbine the water enters in the radial direction but leaves in the axial direction thus it is also called mixed flow type turbine.

As the discharge at outlet is radial $v_{w2} = 0$

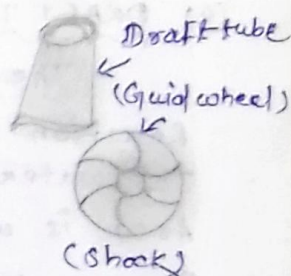
So, work done = $\rho a v_1 [v_{w1} \times u_1]$

Hydraulic efficiency (η_H) = $\frac{v_{w1} \times u_1}{gH}$

$\eta_H = \frac{R.P}{W.P} = \frac{\rho a v_1 [v_{w1} \times u_1]}{\rho \times g \times A \times H} = \frac{v_{w1} \times u_1}{g \times H}$

* Simple definition:-

- it is a reaction turbine.
- it works under the medium head
- it has medium discharge.
- it is Radial flow / mixed flow Turbine.
- it has medium specific speed.

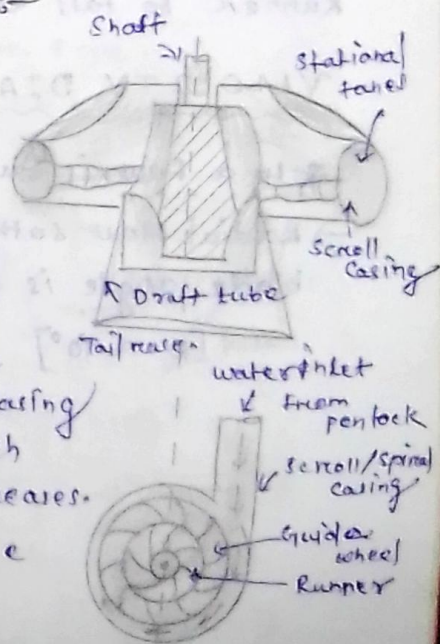


MAIN PARTS OF A FRANCIS TURBINE:-

- (1) casing.
- (2) Guide mechanism.
- (3) Runner with blades.
- (4) Draft tube.

(1) CASING:-

In Francis turbine casing and runner are always full of water. The water from the penstock enters the casing which is spiral/scroll in shape in which area of cross section gradually decreases. The casing completely surrounds the runner of the turbine.



Shorts:-

- In a Francis turbine the casing shape is spiral.
- it is used for to protect the surrounds areas and help to flow water from penstock to runner.
- it is mainly used to protect the existent.

→ The runner is completely enclosed in an air-tight spiral casing.

→ The casing and runner are always full of water.

(2) GUIDE MECHANISM :-

It consists of a stationary circular wheel all round the runner of the turbine. The stationary vanes are fixed on the guide mechanism. The guide vanes allows the water to strike on vane without shock.

(3) RUNNER :-

It is of circular wheel on which a series of radial curved vanes are fixed. Surface of the vanes made very smooth. The radial curve are such that the water enters and leaves without shock.

(4) DRAFT TUBE :-

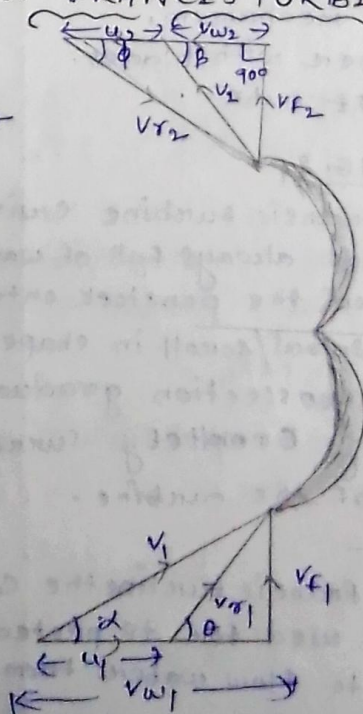
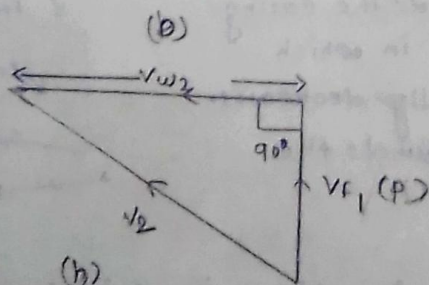
The pressure at the exist of the runner of a reaction turbine is less than atmospheric pressure. The water at exist can't be directly increasing Area is used for discharging water from exist of runner to tail race.

VELOCITY DIAGRAM OF FRANCIS TURBINE :-

* In a francis tube :-

→ Radial flow so the outlet blade angle is 90°

$$\beta = 90^\circ$$



$$\cos \beta = \frac{h}{v_2} = \frac{v_{w2}}{v_2} \Rightarrow \frac{v_{w2}}{v_2} = \cos \beta$$

$$\Rightarrow v_{w2} = v_2 \cos \beta$$

$$= v_2 \cos 90^\circ$$

$$v_{w2} = v_2 = 0$$

RUNNER POWER :-

$$\text{Runner power} = \rho \times Q (v_{w1} + v_{w2}) \times u$$

$$\Rightarrow \rho \times Q (v_{w1} \times u_1 \pm v_{w2} \times u_2) \therefore v_{w2} = 0$$

$$\Rightarrow \rho \times Q (v_{w1} \times u_1)$$

$$R.P = \boxed{\frac{\rho \times Q (v_{w1} \times u_1)}{1000} \text{ kW}}$$

Blade are
not
symmetrical.

HYDRAULIC EFFICIENCY :-

$$\eta_H = \frac{R.P}{\omega \cdot P} = \frac{\rho \times Q (v_{w1} \times u_1)}{\rho \times Q \times g \times H} = \boxed{\frac{v_{w1} \times u_1}{g \times H}}$$

DISCHARGE :-

$$Q = A \times V = \pi D_1 \times B_1 \times V$$

where B_1 = width of the rope.

D_1 = diameter of blades.

HEAD OF FRANCIS :-

$$\text{potential energy} = H = \frac{P}{\rho \times g} \quad [v = \sqrt{2 \times g \times h}]$$

$$\text{Kinetic energy} = \frac{1}{2} \times m \times v^2 \therefore \omega = m \times g$$

$$= \frac{1}{2} \times \frac{\omega}{g} \times v^2 \quad [v^2 = 2 \times g \times h]$$

$$H = \frac{v^2}{2 \times g}$$

$$\text{Total head :- } \boxed{H = \frac{P}{\rho \times g} + \frac{v_1^2}{2g}}$$

or pelton wheel turbine head + $\frac{v_1^2}{2g}$

SOLVED PROBLEMS :-

(1) A Francis turbine working under a head of 15m and the speed of the turbine is 2000 RPM has inlet diameter of 900mm and width is 150mm the constant velocity of flow through the runner is 3m/sec find hydraulic efficiency and inlet blade angle is 90° .

Ans:-

Given data

$H = 15\text{m}$

$N = 2000\text{RPM}$

$D_1 = 900\text{mm} = \frac{900}{1000} = 0.9\text{m}$

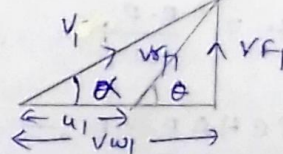
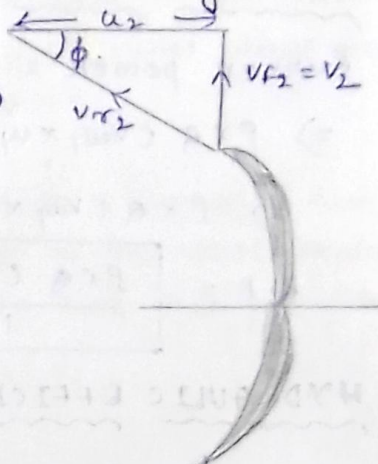
$b = 150\text{mm} = \frac{150}{1000} = 0.15\text{m}$

$V_{f1} = 3\text{m/sec}$ ($V_{f1} = V_{f2}$)

$\eta_H = ?$

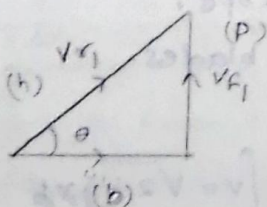
$\theta = 90^\circ$

$\beta = 90^\circ$
 $V_{w2} = 0$



(i) $u_1 = \frac{\pi D N}{60}$

$\Rightarrow \frac{3.14 \times 0.9 \times 2000}{60} = \frac{3.14 \times 0.9 \times 2000}{60} = 9.42\text{m/sec}$



$\sin \theta = \frac{f}{h} = \sin 90^\circ = \frac{V_{f1}}{V_{w1}}$

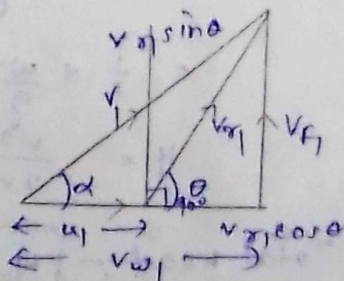
$V_{w1} = \frac{V_{f1}}{\sin 90^\circ} = V_{f1}$

$V_{w1} = u_1 + V_{r1} \cos \theta$

$= 9.42 + 3 \cos 90^\circ$

$= 9.42 + 3 \times 0$

$= 9.42 + 0 = 9.42\text{m/sec}$



$\eta_H = \frac{V_{w1} \times u_1}{g \times H} = \frac{9.42 \times 9.42}{9.81 \times 15}$

$= 60\%$

Ans

(Q) A Francis turbine having overall efficiency of 75% is required to produce 148.25 kW of shaft power. Head is 7.62 m peripheral velocity = $0.26 \sqrt{2gH}$ and Radial velocity at Inlet (Flow) = $0.96 \sqrt{2gH}$, wheel speed is 150 RPM Determine

(1) Find inlet guide blade angle.

(2) Vane angle at inlet.

When the condition of turbine is that there is Hydraulic loss of 22% of Total energy.

Ans:-

Given Data:-

$$\eta_o = 75\% = 0.75$$

$$S.p = 148.25 \text{ kW}$$

$$H = 7.62 \text{ m}$$

$$u = 0.26 \sqrt{2gH}$$

$$V_{f1} = 0.96 \sqrt{2gH}$$

$$N = 150 \text{ RPM}$$

$$(1) V_1 = \sqrt{2 \times g \times H} = 12.22 \text{ m/sec}$$

$$(2) u_1 = 0.26 \sqrt{2 \times g \times H} = 3.17 \text{ m/sec}$$

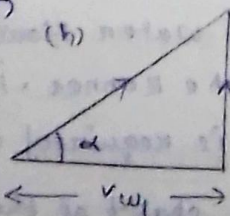
$$(3) V_{f1} = 0.96 \sqrt{2 \times g \times H} = 11.73 \text{ m/sec}$$

$$(4) \eta_H = \frac{V_{w1} \times u_1}{g \times H}$$

$$\text{(condition)} \eta_H = 100 - 22 = 78\% = 0.78$$

$$\Rightarrow 0.78 = \frac{V_{w1} \times 3.17}{9.81 \times 7.62} = V_{w1} = 18.39 \text{ m/sec}$$

(5)



(b)

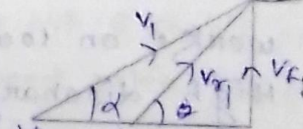
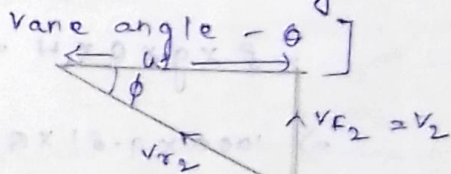
$$\tan \alpha = \frac{p}{b} = \frac{V_{f1}}{V_{w1}}$$

$$= \frac{11.73}{18.39} = 0.63 = \tan^{-1} 0.63$$

$$\Rightarrow \alpha = 32.2^\circ$$

(Blade speed - peripheral velocity)

[Inlet guide blade angle - α



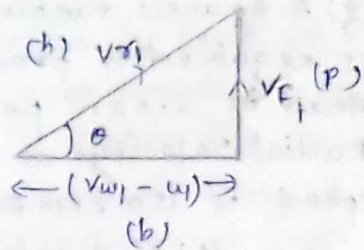
(6)

$$\tan \theta = \frac{P}{b} = \frac{V_{F1}}{(V_{w1} - u)}$$

$$\Rightarrow \frac{11.73}{(18.29 - 3.17)}$$

$$\Rightarrow 0.77 \Rightarrow \tan^{-1} 0.77$$

$$\theta = 37.5^\circ$$



(7) Dis charge :-

$$\eta_o = \frac{S.P}{W.P} = 0.75 = \frac{148.25}{W.P}$$

$$W.P = \frac{148.25}{0.75} = 197.66 \text{ kW}$$

$$= \rho \times g \times Q \times H = 197.66 \times 1000$$

$$\Rightarrow 1000 \times 9.81 \times Q \times 7.62 = 197.66 \times 1000$$

$$Q = \frac{197.66 \times 1000}{1000 \times 9.81 \times 7.62} = \frac{197.66 \times 1000}{74752.2}$$

$$\Rightarrow 2.64 \text{ m}^3/\text{sec}$$

Ans

KAPLAN TURBINE

* ~~~~~ *

- It is an axial flow turbine.
- works on low head (5m-10m)
- High discharge.
- Very high specific speed.
- comes under the reaction turbine.

* It is axial flow turbine it means water flows parallel to the axis of rotation of the runner. It is used when large volume of water is required at low head for axial flow turbines the shaft of the turbine is vertical. The lower end of the shaft is made larger which is known as hub/Boss

* PROPELLOR & KAPLAN TURBINE :-

When the vanes are fixed on the hub it's called as propellor turbine, when they are adjustable it's called as Kaplan Turbine.

→ The turbine extracts energy from a moving fluid, while the other two add energy to a moving fluid.

DISCHARGES :-

$$Q = A \times V$$

$$\text{Area} = \frac{\pi}{4} \times d^2$$

$$\Rightarrow \frac{\pi}{4} \times (D_R^2 - D_B^2) \times V$$

since this is an axial flow type $V_{f1} = V_{f2}$

$$Q_{\text{Kap}} = \frac{\pi}{4} \times (D_R^2 - D_B^2) \times V_{f1}$$

where,

D_R = Dia. of the runner.

D_B = Dia. of the boss.

Blade speed ($u_1 = u_2$)

$$u = \frac{\pi D N}{60} = \frac{\pi D R N}{60}$$

SOLVED PROBLEMS :-

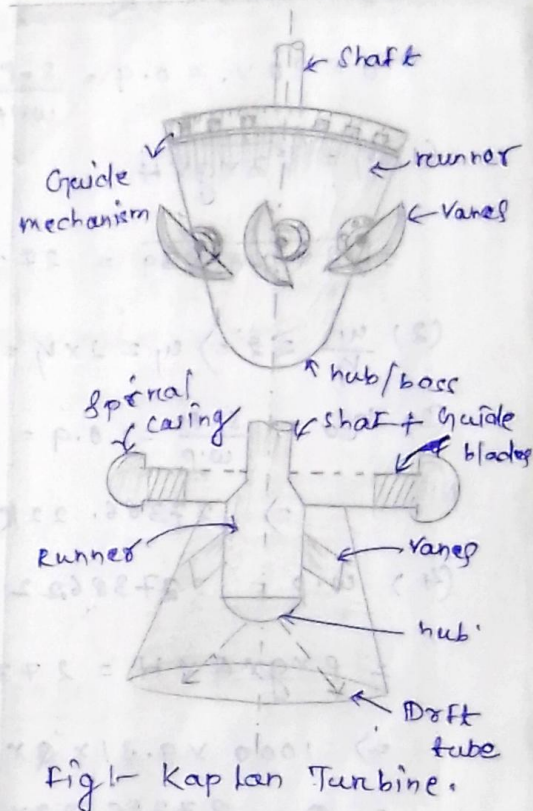
(1) A Kaplan turbine develop 24,647.6 kW of power at a head of 39 m. Assuming speed ratio of 2, flow ratio 0.6 diameter of the boss is equal to 0.35 times the diameter of the runner and overall efficiency is 90%. Calculate diameter of hub and runner and the speed of the turbine.

Ans :-

Given Data :-

$$S.P = 24,647.6 \text{ kW}$$

$$H = 39 \text{ m}$$

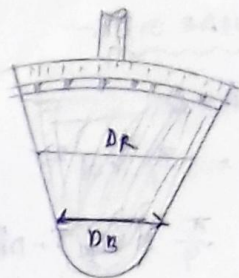


$$\text{Speed ratio} = \frac{\text{Blade}}{\text{water jet}} = \frac{u_1}{V_1} = 2$$

$$\text{Flow Ratio} = \frac{\text{Velocity of flow at inlet}}{\text{water jet velocity}} = 0.6 = \frac{V_{f1}}{V_1}$$

$$D_B = 0.35 \times D_R$$

$$\eta_o = 90\% = 0.9 = \frac{\text{S.P}}{\text{W.P}}$$



$$(1) V_1 = \sqrt{2 \times g \times H}$$

$$= \sqrt{2 \times 9.81 \times 39} = 27.66 \text{ m/sec.}$$

$$(2) \frac{u_1}{V_1} = 2 \Rightarrow u_1 = 2 \times V_1 = 2 \times 27.66 = 55.32 \text{ m/sec.}$$

$$(3) \eta_o = \frac{\text{S.P}}{\text{W.P}} \Rightarrow 0.9 = \frac{24647.6}{\text{W.P}} \Rightarrow \text{W.P} = \frac{24647.6}{0.9}$$

$$\Rightarrow 27386.22 \text{ kW}$$

$$(4) \text{W.P} = 27386.22 \text{ kW}$$

$$= \rho \times g \times Q \times H = 27386.22 \times 10^3$$

$$\Rightarrow 1000 \times 9.81 \times Q \times 39 = 27386.22 \times 1000$$

$$= Q = \frac{27386.22 \times 1000}{1000 \times 9.81 \times 39} = \frac{27386.22}{9.81 \times 39}$$

$$\Rightarrow 71.58 \text{ m}^3/\text{sec}$$

$$(5) \frac{V_{f1}}{V_1} = 0.6 \Rightarrow V_{f1} = 0.6 \times V_1$$

$$\Rightarrow 0.6 \times 27.66$$

$$\Rightarrow 16.59 \text{ m/sec}$$

$$(6) Q = A \times V$$

$$\Rightarrow \frac{\pi}{4} \times (D_R^2 - D_B^2) \times V_{f1}$$

$$\Rightarrow 71.58 = \frac{\pi}{4} \times (D_R^2 - (0.35 \times D_R)^2) \times 16.59$$

$$\Rightarrow 71.58 = \frac{\pi}{4} \times D_R^2 (1 - 0.122) \times 16.59$$

$$\Rightarrow 71.58 = \frac{\pi}{4} \times D_R^2 \times 0.878 \times 16.59$$

$$\Rightarrow 71.58 = 0.785 \times 0.878 \times 16.59 \times D_R^2$$

$$\Rightarrow 71.58 = 11.43 \times D_R^2$$

$$\Rightarrow D_R^2 = \frac{71.58}{11.43} \Rightarrow D_R = 2.50$$

$$\Rightarrow D_R = \sqrt{6.26} = 2.50 \text{ m}$$

$$\Rightarrow D_B = 0.35 \times D_R$$

$$\Rightarrow 0.35 \times 2.50 = 0.875 \text{ m}$$

$$(7) \text{ Speed } = 4, \Rightarrow \frac{\pi D R N}{60} = \frac{3.14 \times 2.5 \times N}{60}$$

$$\Rightarrow 55.32 = 0.130 \times N$$

$$N = \frac{55.32}{0.130} = 425.53 \text{ RPM}$$

Ans

PUMP

16/09/2023

* Pump:- It is a hydraulic machine, which is convert mechanical energy to hydraulic energy.

Types:-

(1). Reciprocating pump. (Reciprocating motion of piston T.D.C to B.D.C.)

(2). Centrifugal pump. (Impeller - Rotating element).

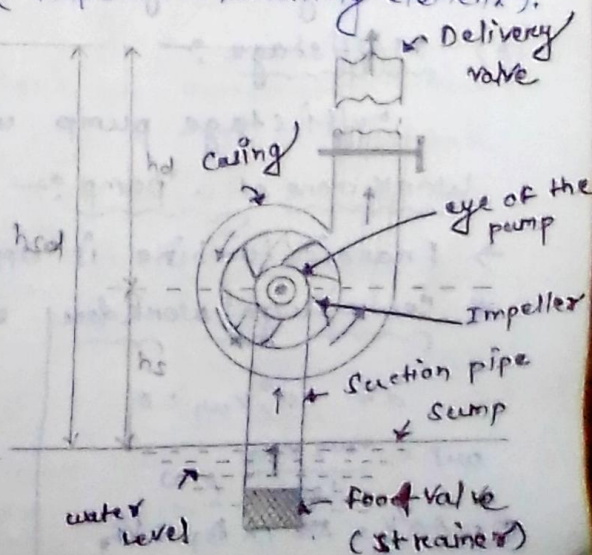
(2). CENTRIFUGAL PUMP

IMPORTANT PARTS:-

- 1 - Casing
- 2 - eye of the pump
- 3 - Impeller
- 4 - Sump

* Suction pipe:-

→ Create pressure difference (vacuum).



* h_s : From water level to eye of the pump, is known as Suction head (h_s).

* h_d : From eye of the pump to delivery pipes is known as Delivery head (h_d).

* Total head (suction head + Delivery head) is known as static head (h_{sd}).

* MANOMETRIC HEAD:— (Actual head).

→ (Head loss due to friction in both pipes)

↓
Suction
(h_{fs})

↓
Discharge
(h_{fd})

$$H_m = h_s + h_d + h_{fs} + h_{fd} + \frac{v^2}{2g}$$

Where,

h_s = Suction head.

h_d = Discharge head.

H_m = manometric head.

h_{fs} = Suction head loss due to friction.

h_{fd} = Discharge head loss due to friction.

$\frac{v^2}{2g}$ = water head, (Kinetic energy).

Single stage & Multi stage:—

(1) single stage :- (pump)

A single stage pump uses one impeller.

(2) Multi stage :-

Multi stage pump uses 2 or more impellers.

Work done of a pump :-

→ Francis' turbine is opposite of centrifugal pump.

* Centrifugal work done

$$d = 90^\circ, v_{w1} = 0$$

$$W.D = \frac{v_{w2} \times u_2}{1000} \text{ kW}$$

$$Q = A \times V = \pi R D_1 \times D_2 \times V_{f1}$$

* Francis turbine :-

Radial discharge

$$\phi = 90^\circ, v_{w2} = 0$$

$$W.D = \frac{v_{w1} \times u_1}{1000}$$

PRIMING :-

It is the process of Filling the pipe and casing with water so that the air accumulated in the pipe can be removed and the function on the pump becomes normal.

CASING SHAPES :-

1. - Spiral
2. - Volute
3. - Vertex

$$\left[\begin{aligned} K.E &= \frac{v^2}{2 \times g} \quad \rightarrow \text{pressure energy} \\ &= \frac{(\omega \times r)^2}{2 \times g} = \frac{\omega^2 r^2}{g} \quad \left[\begin{array}{l} v = \omega \times r \\ \downarrow \\ \text{linear velocity} \end{array} \right. \end{aligned} \right.$$

* EFFICIENCIES OF CENTRIFUGAL PUMP :-

(1). Manometric efficiency :-

$$\eta_{\text{mano}} = \frac{\text{Manometric head}}{\text{Impeller head}}$$

(2). Mechanical efficiency :-

$$\eta_{\text{mech}} = \frac{\text{Impeller power}}{\text{Shaft power}}$$

(3). Overall efficiency :-

$$\eta_o = \eta_{\text{mano}} \times \eta_{\text{mech}}$$

(1). Manometric efficiency :-

$$\eta_{\text{mano}} = \frac{h_m}{I.h} = \frac{(h_s + h_{dt} + h_{fs} + h_{fd} + \frac{v^2}{2g})}{\frac{v_{w2} \times u_2}{g}}$$

$$= \frac{g \times h_m}{v_{w2} \times u_2}$$

where, h_m = manometric head,
 $I.h$ = Impeller head.

(2). Mechanical efficiency :-

$$\eta_{\text{mech}} = \frac{I.P}{S.P} = \frac{\frac{v_{w2} \times u_2}{g}}{\frac{2\pi NT}{60}} = \boxed{\frac{v_{w2} \times u_2}{g} \times \frac{60}{2\pi NT}}$$

where, I.P = Impeller Power
S.P = Shaft power.

(3). Overall efficiency:-

$$\eta_o = \eta_{mano} \times \eta_{mech} = \frac{h_m}{\frac{v_{w2} \times u_2}{g}} \times \frac{\frac{v_{w2} \times u_2}{g}}{\frac{2\pi NT}{60}} = \frac{h_m}{S.P}$$

$$= \frac{h_s + h_d + h_{fs} + h_{fd} + \frac{v^2}{2g}}{\frac{2\pi NT}{60}}$$

$$\Rightarrow \boxed{\frac{60 (h_s + h_d + h_{fs} + h_{fd} + \frac{v^2}{2g})}{2\pi NT}}$$

SOLVED PROBLEMS:-

(Q₁) In a Centrifugal pump. the manometric and mechanical efficiencies are 75% and 85%. Find out the overall efficiency?

Ans:-

Given data

$$\eta_{mano} = 75\% = 0.75$$

$$\eta_{mech} = 85\% = 0.85$$

we know that overall efficiency

$$\eta_o = \eta_{mano} \times \eta_{mech} = 0.75 \times 0.85$$

$$= 0.6375 \approx 63.75\%$$

✓ (Vortex Casing)

Ans

(Q₂) In a Centrifugal pump internal and external dia of the impeller are 200 mm and 400 mm. The pump is rotating at 1200 rpm. The vane angle at inlet and outlet is 20° and 30°. The water enters radially and velocity of flow is constant. Find the work done by the impeller (unit weight of water).

Ans:-

Given Data

$$d = 200 \text{ mm} = \frac{200}{1000} = 0.2 \text{ m}, \quad N = 1200 \text{ r.p.m.}$$

$$D = 400 \text{ mm} = \frac{400}{1000} = 0.4 \text{ m}$$

$$\theta_1 = 20^\circ$$

$$\phi_2 = 30^\circ$$

When Radial flow $\alpha = 90^\circ$, $v_{w1} = 0$

$$v_{f1} = v_{f2}$$

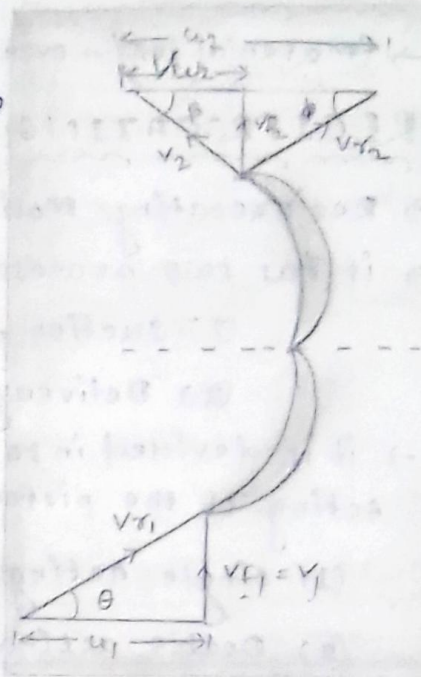
We know that

$$\omega = \frac{\pi d N}{60} = \frac{\pi \times 0.2 \times 1200}{60}$$

$$\Rightarrow 12.56 \text{ m/sec}$$

$$u_2 = \frac{\pi D N}{60} = \frac{\pi \times 0.4 \times 1200}{60}$$

$$\Rightarrow 25.13 \text{ m/sec}$$



We know that work done

$$W.D = \frac{v_{w2} \times u_2}{g}$$

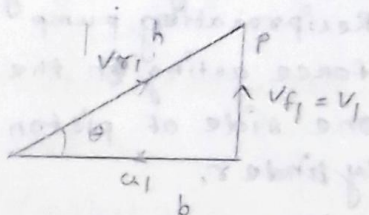
* Inlet velocity triangle :-

$$\tan \theta = \frac{p}{b} = \tan 20^\circ = \frac{v_{f1}}{u_1}$$

$$\Rightarrow v_{f1} = u_1 \times \tan 20^\circ$$

$$\Rightarrow v_{f1} = v_{f2}$$

$$\Rightarrow \frac{v_{f1}}{u_1} = \frac{v_{f1}}{12.56} = 4.47 \text{ m/s}$$

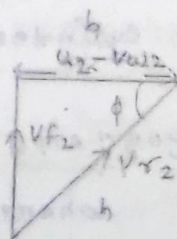


* Outlet velocity triangle :-

$$\tan \phi = \frac{v_{f2}}{u_2 - v_{w2}}$$

$$= \frac{4.47}{25.13 - v_{w2}} = \tan 30^\circ$$

$$= v_{w2} = 17.215 \text{ m/s}$$



\(\therefore\) work done by the impeller per kg of water per second

$$\Rightarrow \frac{v_{w2} \times u_2}{g} = \frac{17.215 \times 25.13}{9.81} = 44.2 \text{ N}$$

Ans

CAVITATION:-

→ (Material) loss - over water is straight on blade)

RECIPROCATING PUMP:-

→ Reciprocating Motion of piston T.D.C to B.D.C.

→ It has two processes is

(1) Suction process.

(2) Delivery process.

→ it is divided into two type according to the force acting of the piston cylinder:-

(1) single acting Reciprocating pump.

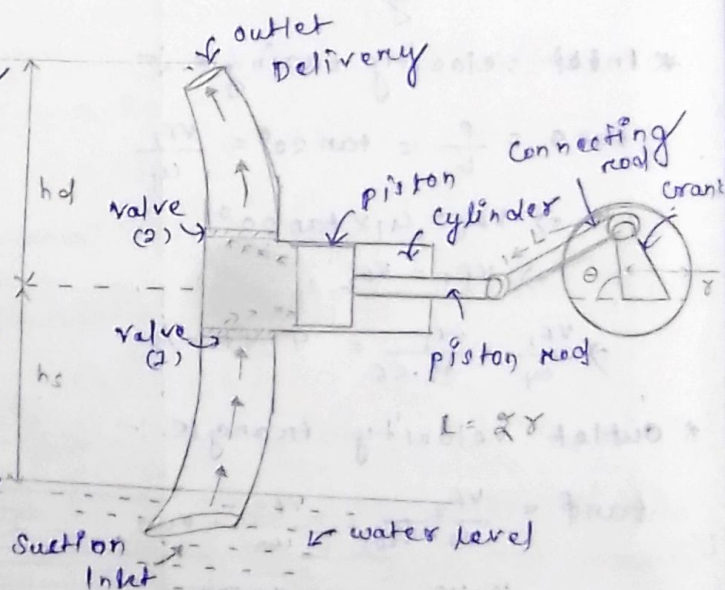
(2) Double acting Reciprocating pump.

(1) single Acting Reciprocating pump:-

→ In a single acting Reciprocating pump force acting in the one side of piston cylinder.

→ it has one inlet & one outlet.

→ it is low discharge comparison of double acting cylinder.



→ Total head = $h_s + h_d$

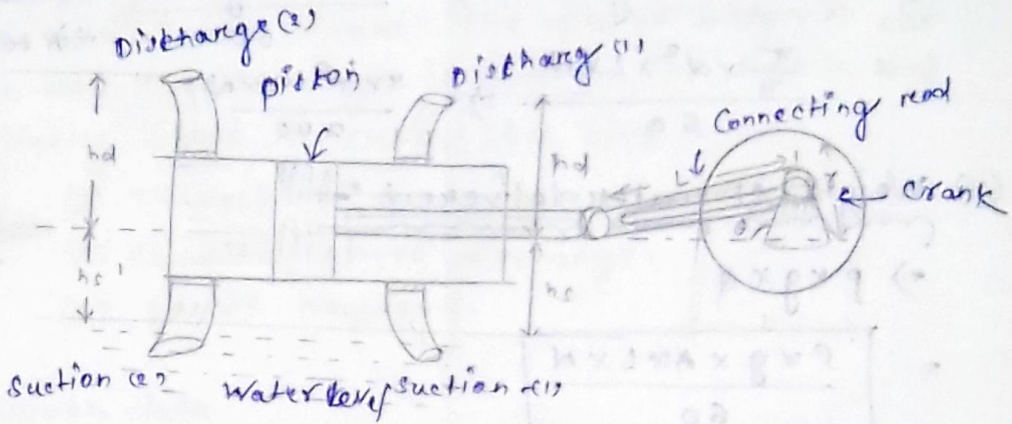
where, h_s = suction head

h_d = delivery head.

(2) Double acting Reciprocating pump:-

→ In a Double acting reciprocating pump force acting in the both side of piston cylinder.

- it has two inlet & outlet ways.
- it is used for generate high discharge.
- Total head = $2 \times (h_s + h_d)$.



* DIFFERENCE BETWEEN CENTRIFUGAL & RECIPROCATING PUMP *

CENTRIFUGAL PUMP	RECIPROCATING PUMP
1. due to Centrifugal Force	1. due to reciprocating motion of piston T.D.C to B.D.C.
2. used Impeller to generate power.	2. used engine to generate power.
3. Low maintainess required.	3. High maintainess required.
4. Low Cost	4. High Cost
5. Low discharge	5. high discharge.
6. Less pollution	6. high pollution Comparison of centrifugal pump.

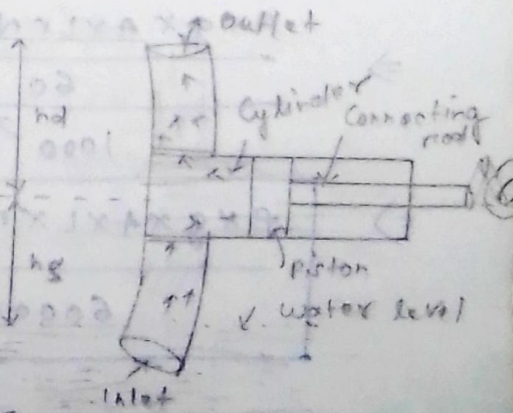
DISCHARGE IN SINGLE ACTING RECIPROCATING PUMP

- r = radius of crank
- $L = 2r$ (Length of the stroke)
- $A = \frac{\pi}{4} d^2$ (d = piston or cylinder)

(1) Volume of water delivered:-

$$= A \times L \Rightarrow \frac{\pi}{4} d^2 \times L$$

where, A = Area of the cylinder.
 L = length of the stroke.



(2). "Q" = discharge :-

$$Q = \text{Area} \times \text{Length} \times N \Rightarrow \frac{\text{Area} \times \text{Length} \times N}{60} \quad (\text{to convert min to sec})$$
$$= \frac{\frac{\pi}{4} \times d^2 \times L \times N}{60} \Rightarrow \frac{\pi \times d^2 \times L \times N}{240}$$

(3). Weight of water delivered :-

$$\Rightarrow \rho \times g \times Q$$

$$= \boxed{\frac{\rho \times g \times A \times L \times N}{60}}$$

(4). Work done by single acting reciprocating pump :-

$$\boxed{W = \text{force} \times \text{displacement}} \quad (\text{work done} = \text{force} \times \text{distance travel})$$

$$\Rightarrow \text{weight of water delivered} \times (h_s + h_d)$$

$$= \rho \times g \times Q \times (h_s + h_d)$$

$$= \boxed{\frac{\rho \times g \times A \times L \times N \times (h_s + h_d)}{60}}$$

(5). power delivered :-

$$P = \frac{\text{work done}}{1000} \quad \left\{ \begin{array}{l} \text{According to the law of machine} \\ \text{According to the law of mechanics} \\ \downarrow \\ \left(\frac{\text{work done}}{\text{time}} \right) \end{array} \right.$$

$$\Rightarrow \frac{\rho \times g \times A \times L \times N \times (h_s + h_d)}{60} \times \frac{1}{1000}$$

$$\Rightarrow \boxed{\frac{\rho \times g \times A \times L \times N \times (h_s + h_d)}{60000} \text{ kw}}$$

SOLVED PROBLEMS:-

problem-1:- A single acting reciprocating pump running at a speed of 60 rpm delivers water at 0.53 m^3 per minute. The dia. of piston is 200 mm and stroke length is 300 mm. The suction and delivery head is 4m and 12m. find:

- (1) Theoretical discharge.
- (2) Co-efficient of discharge.
- (3) power required.

Ans:-

Given data

$$N = 60 \text{ rpm}$$

$$Q = 0.53 \text{ m}^3/\text{min} = \frac{0.53}{60} = 0.008833 \text{ m}^3/\text{sec.}$$

$$d = 200 \text{ mm} = \frac{200}{1000} = 0.2 \text{ m}$$

$$L = 300 \text{ mm} = \frac{300}{1000} = 0.3 \text{ m}$$

$$h_s = 4 \text{ m}$$

$$h_d = 12 \text{ m}$$

We know that

$$A = \frac{\pi}{4} \times d^2 = \frac{\pi}{4} \times (0.2)^2 = 0.0314 \text{ m}^2$$

(1) Discharge (theoretical) :-

$$Q = \frac{A \times L \times n}{60} = \frac{0.0314 \times 0.3 \times 60}{60} \\ = 0.00942 \text{ m}^3/\text{sec.}$$

(2) Co-efficient of discharge :-

$$C_d = \frac{Q_{\text{actual}}}{Q_{\text{theoretical}}} = \frac{0.008833}{0.00942}$$

$$C_d = 0.934$$

(3). power delivered :-

$$= \frac{\rho \times g \times Q \times (h_s + h_d)}{1000}$$

$$= \frac{1000 \times 9.81 \times 0.00942 \times (4 + 12)}{1000}$$

$$= 9.81 \times 0.00942 \times 16$$

$$= 1.478 \text{ Kw}$$

Ans

* WORK done by double acting reciprocating pump :-

D = piston diameter

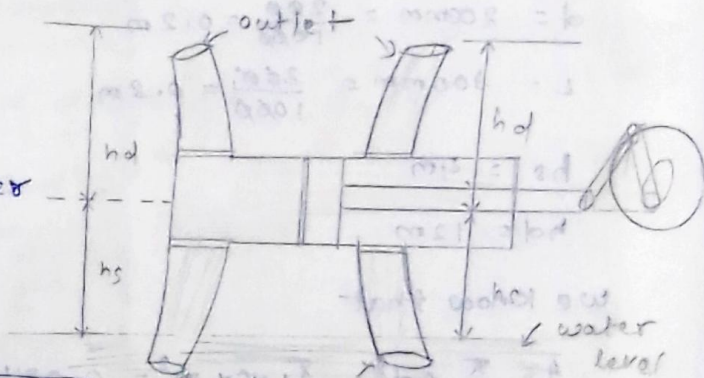
$$\Rightarrow \frac{\pi}{4} \times D^2$$

d = piston rod diameter

$$\Rightarrow \frac{\pi}{4} \times (D^2 - d^2)$$

Total Area :-

$$\Rightarrow \boxed{\frac{\pi}{4} \times D^2 + \frac{\pi}{4} \times (D^2 - d^2)}$$



(1). Volume of water delivered :-

\Rightarrow Area \times length of the stroke.

$$= \boxed{\frac{\pi}{4} \times D^2 + \frac{\pi}{4} \times (D^2 - d^2) \times L}$$

(2) Discharge :-

$$Q = \frac{A \times L \times N}{60} =$$

$$\boxed{\frac{\frac{\pi}{4} \times D^2 + \frac{\pi}{4} \times (D^2 - d^2) \times L \times N}{60}}$$

CONDITION:-

IF the diameter of the piston rod can be neglected.

(1) Discharge:-

$$Q = \frac{\left(\frac{\pi}{4} \times D^2 + \frac{\pi}{4} \times d^2\right) \times L \times N}{60}$$

$$\Rightarrow \frac{2 \times \frac{\pi}{4} \times D^2 \times L \times N}{60}$$

$$\Rightarrow \frac{2 \times A \times L \times N}{60}$$

(2) work done:-

\Rightarrow force \times displacement

= weight of water delivered \times (hs + hd)

$$= 2 \times \rho \times g \times Q \times (h_s + h_d) \quad \text{(power delivered):-}$$

$$= \frac{2 \times \rho \times g \times A \times L \times N \times (h_s + h_d)}{1000} \quad \text{kw}$$

SLIP IN RECIPROCATING PUMP:-

slip = $\frac{\text{Theoretical discharge} - \text{Actual discharge}}{\text{Theoretical discharge}}$

$$\text{Negative slip} = \frac{Q_{\text{theo}} - Q_{\text{actual}}}{Q_{\text{theo}}}$$

* slip is percentage:-

$$\text{slip} = \frac{Q_{\text{th}} - Q_{\text{act}}}{Q_{\text{th}}} \times 100 \Rightarrow 1 - \frac{Q_{\text{act}}}{Q_{\text{th}}} \times 100$$

$$= (1 - \text{cd}) \times 100$$

$$\left[\text{cd} = \frac{Q_{\text{actual}}}{Q_{\text{theoretical}}} \right]$$

INDUSTRIAL FLUID POWER:-

In the fluid power industries, fluid is used to generate power and this power can be utilised in various industries.

Types:-

- (1) Hydraulic Control System.
- (2) Pneumatic Control System.

(1) Hydraulic Control System:-

In hydraulic control system. Hydraulic oil is used to generate power, with the help of pump.

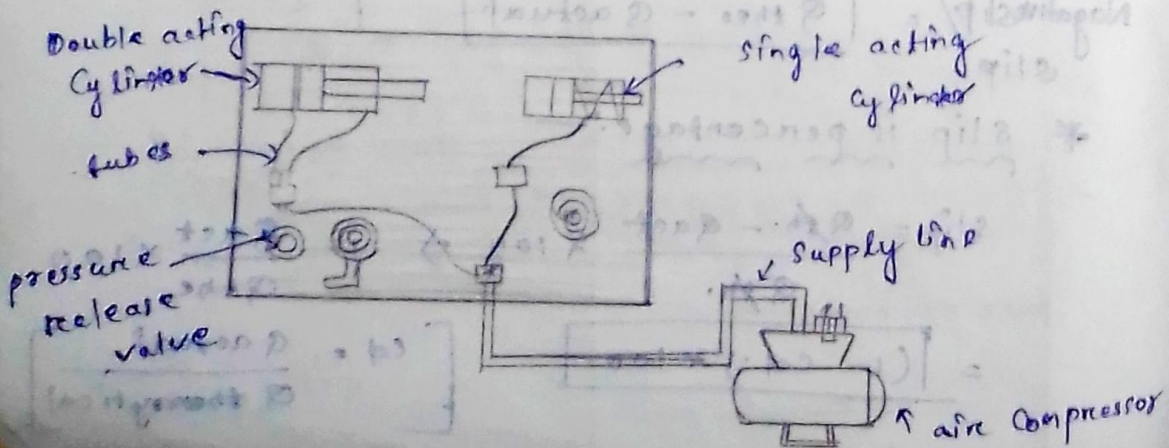
- In this control system the capacity of power generation is high.
- it is widely used in bigger industrial application.

(2) Pneumatic Control System:-

In pneumatic control system. Air is used to generate power, with the help of Air Compressor.

- it is widely used in smaller industrial application.

(2). PNEUMATIC CONTROL SYSTEM:-



ELEMENTS OF PNEUMATIC CONTROL SYSTEM:-

(1) Compressor:-

It takes the air from the atmosphere then compress it and supply to the pneumatic system. Various types of compressor can be used according to the required operation.

Types of compressor:-

(1). Reciprocating/compression.

- (i) single stage/multi stage.
- (ii) single acting / Double acting.

(2). Rotary type:-

- (i) centrifugal pump.

(3). Flow type:-

- (i) Axial flow.
- (ii) Radial flow.

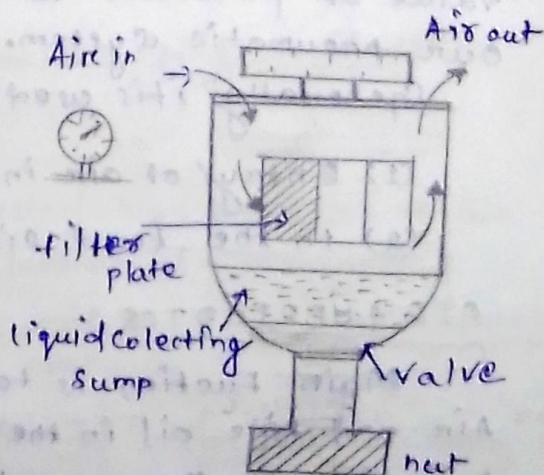
(4). Diaphragm type:-

→ Here piston and cylinder section is delivered by a Diaphragm.

PARTS OF COMPRESSOR PARTS:-

(1). Air filter:-

→ It allows pure air to the compressor by restricting moisture, dust particle, water particle etc.



* Important parts used to filter and heat control in Pneumatic system:-

(1). Inlet Filter:-

→ 1st protecting device of pneumatic control system,

→ it is protect from dust, moisture etc.

(2). After - Cooler:- (Tube types)

Types:- (1) water cooler

(2) Air cooler.

(3). Inter - cooler:-

→ Cooling system used in different stages of Compressor. it is in tubular form.

AIR DRYERS:-

→ when the air contains moisture in large amount Air dryers are used to soak the water vapour from air.

REGULATOR:-

It is used to regulate the pressure of air when there is fluctuation in air pressure, It keeps the value of pressure at a value which is safe for our pneumatic system.

Generally it is used in

(1) Entry of air into pneumatic.

(2) In the load circuit.

AIR LUBRICATOR:-

Main function is to supply the mixture of Air and fine oil in the form of spray to that friction in the machine parts can be reduced.

Generally it is used in

(1) valves, (2) machine packings, (3) other moving parts

MUFFLER:-

It is also called silencer, which is used to reduce the noise of the outlet high pressure of air. It is the form of a small cylindrical nut which is tightened on the outlet of air.

They are made from Bronze material.

FRL UNIT:-

- F = Filter
- R = Regulator
- L = Lubricator.

PNEUMATIC ACTUATOR:-

- Actuators are the components which convert one form of energy to another form of energy.
- Here the high pressure of air is converted to mechanical action.
- In pneumatic system actuators are divided into two types:

- (1) Linear
- (2) Rotary.

(1). Linear:-

The action will be in linear or Reciprocating types.

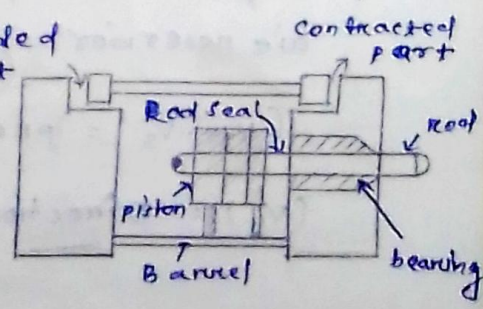
Ex:- single acting & Double acting cylinders.

(2). Rotary type:-

Here the compressed high pressure of air produced the rotary motion the mechanical system.

Ex:- Air motors.

Double acting Cylinder:-



PRESSURE CONTROL VALVE :-

→ PCV :- Basically in pneumatic control system pressure control valves are used for safety purpose their main objective is to provide pressure of air within certain limit. Various condition arises while operating are:

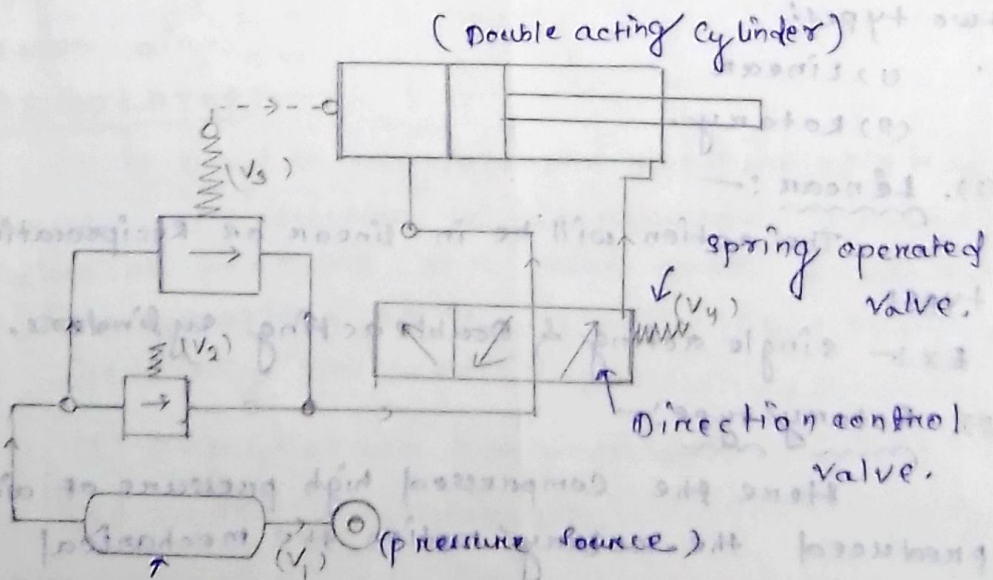
- high pressure in the circuit.
- Low pressure in the circuit.
- Delivery pressure is very high local fluctuation.

Valves :-

- (1) Non return valve.
- (2) Spring operated valve.
- (3) Needle operated valve.

CASE - I

PROTECTION AGAINST LOW PRESSURE :-



(V_1 = Non-return valve)

($V_2 - V_3$) = pressure control valve)

(V_4) = Direction Control Valve - DCV

Direction Control Valve (DCV):

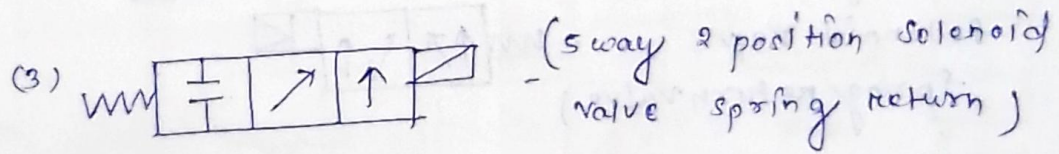
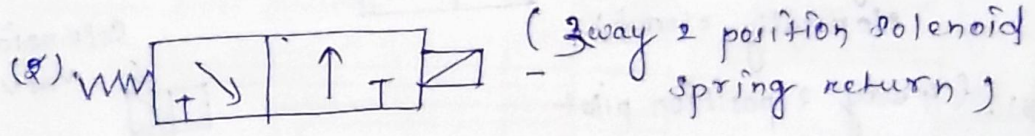
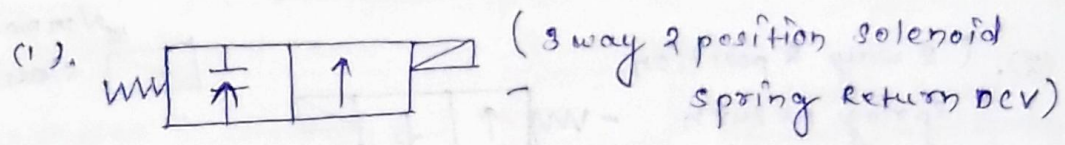
In pneumatic control system direction valves are used to control the direction of flow generally these valve are either hand operated or solenoid operated.

These are classified based upon the inlet and outlet condition of air like

- (i) 2 way 2 direction.
- (ii) 3 way 2 direction.

(T = Block path)

(way - inlet, outlet)


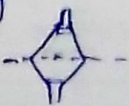
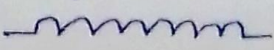


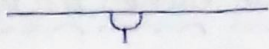
PNEUMATIC SYMBOLS:

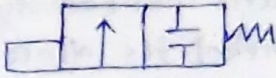
* All are ISO (indian standard organization) symbols:

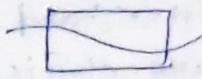
- (1) pressure port (P).
- (2) Drain port (L).
- (3) working port (A, B, C).
- (4) Exhaust port (R, S, T).

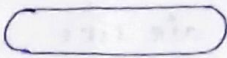
Symbols used in pneumatic system:

- (1). pressure gauge - 
- (2). Cooler - 
- (3). coil tube - 

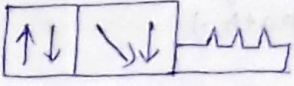
(4). Connection point - 

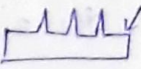
(5). 3/4 mechanical valve - 

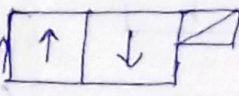
(6). Solenoid activator - 

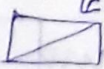
(7). Reservoir - 

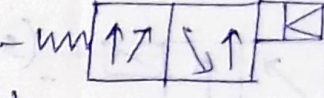
Valve operation diagram:-


(1). (4 way 2 position manual control) - 

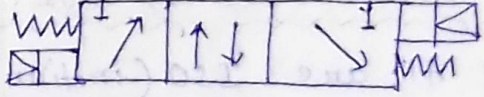
 manual control.

(2). (2 way 2 position spring return Normally closed) - 

 Normally closed

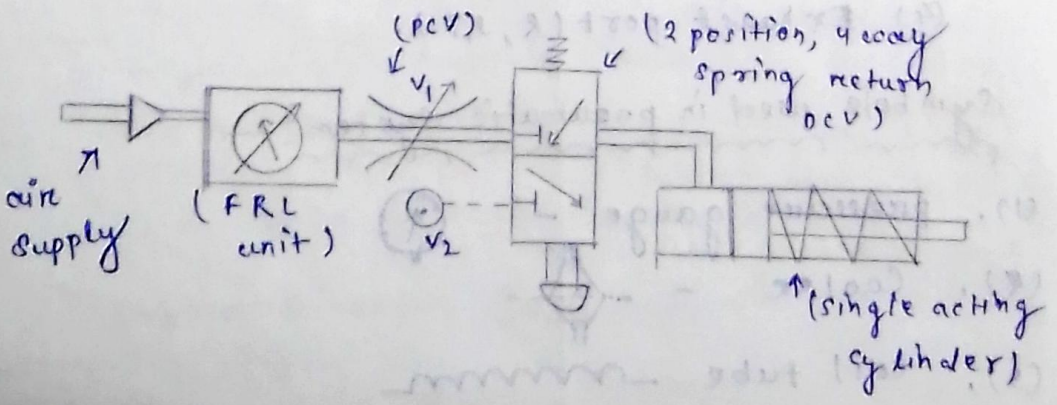
(3). (4 way 2 position pilot solenoid valve spring return valve.) - 

 Solenoid valve.

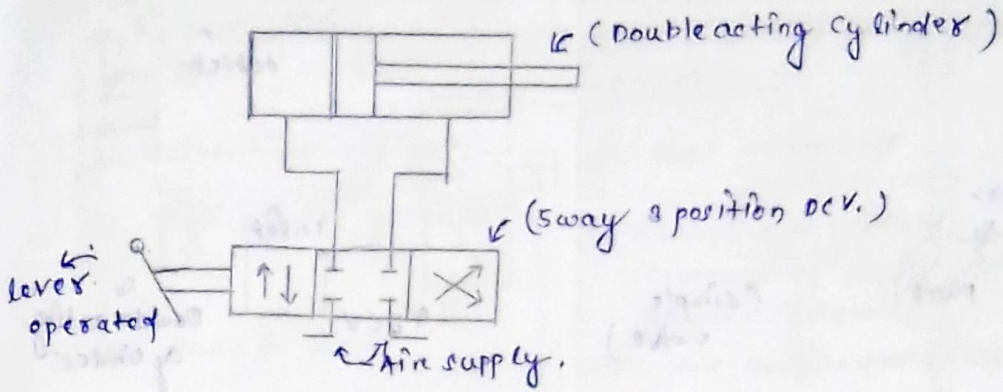
(4). (4 way (5 port) position spring return centre, Double-pilot solenoid valve.) - 

Circuit diagram to control pneumatic components :-

(1) Operate single acting cylinder:-



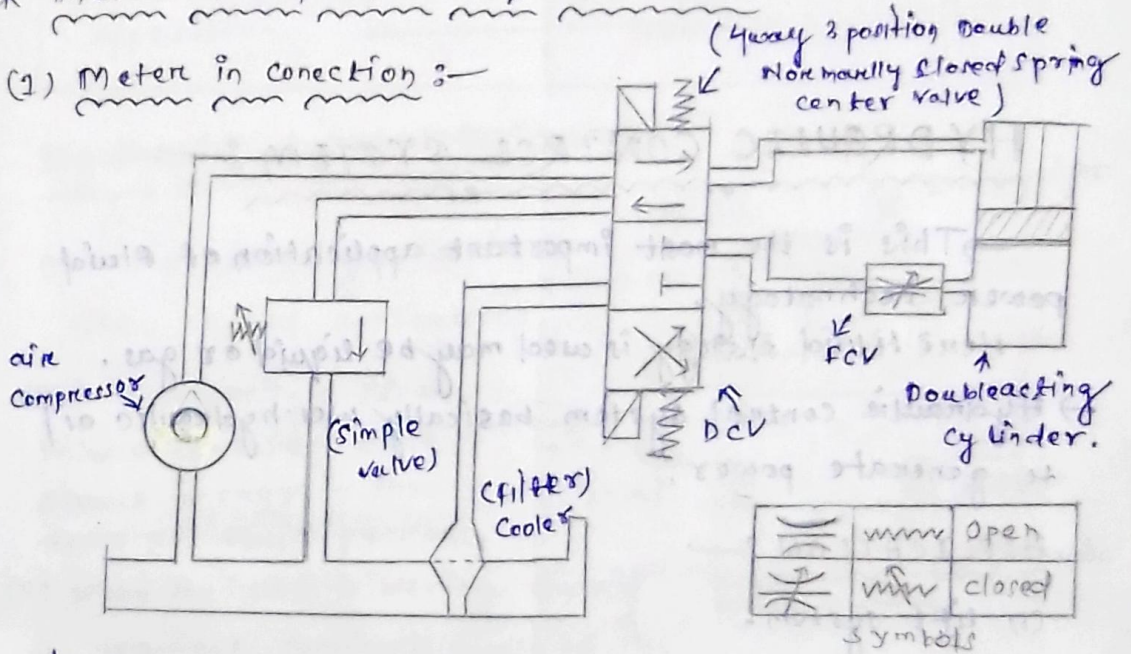
(2) operate double acting cylinder :-



Operation on double acting cylinder :-

* meter-in and meter-out Connection :-

(1) Meter in connection :-



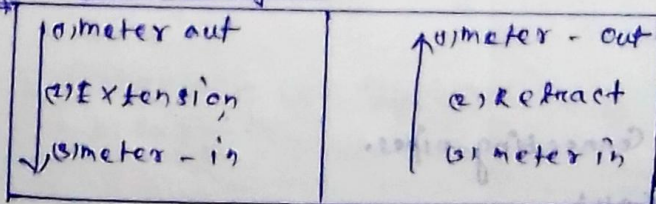
* it has two processes :-

- (1) extension
- (2) retraction

* FCV = flow control valve - (fluid).

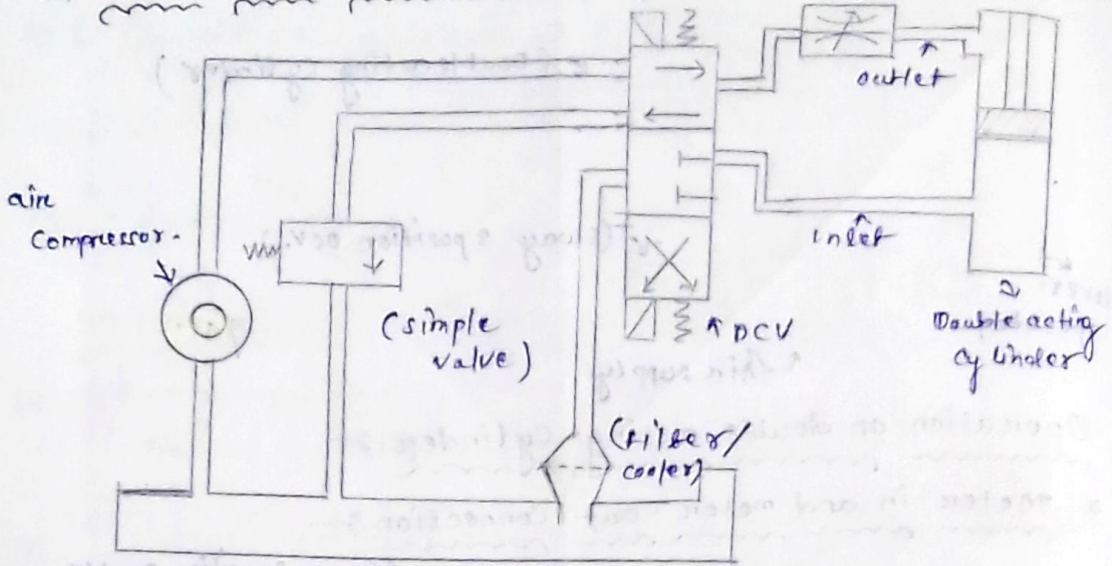
meter-in - on
 meter-out - off
 (conditions)

(MQ) Circuit diagram



(2) meter-out connection:

(4-way 3-position double normally closed, spring centre valve) & FCV



HYDRAULIC CONTROL SYSTEM

→ This is the most important application of fluid power technology.

→ Here, fluid is used may be liquid or gas.

→ Hydraulic control system basically uses hydraulic oil to generate power.

APPLICATION:

- (1) Lift system.
- (2) cranes and hoist.
- (3) industrial application
- (4) operate single / double acting cylinders.

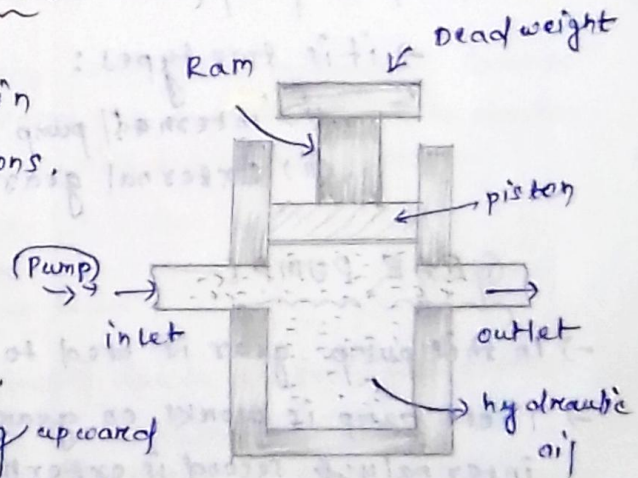
Important parts in hydraulic control system:

- (1) Hydraulic oil
- (2) pump.
- (3) high quality connecting pipes.
- (4) Valves (DCV, FCV)
- (5) Actuators (single acting / double acting cylinders).
- (6) FRL unit (Filter, regulator, lubricator).

Hydraulic	Pneumatic
(1). hydraulic oil used to generate power.	(1) Air is used to generate power.
(2). maintainers is high	(2). less maintainers,
(3). High power generate	(3) low power generat comparison of hydraulic control system.
(4). Pump is used	(4). Air compressor is used
(5). High Cost	(5). low cost.
(6). used in bigger industrial Application	(6). used in smaller industrial application

Hydraulic Accumulator :-

- (1) it is basically used in lift; cranes applications.
- (2) it is generally a fixed volume container which stores energy in the form of fluid pressure.
- (3) when the lift is moving upward it requires continuous supply of hydraulic oil.



Pump in Hydraulic Control System :-

it is a hydraulic machine which it convert mechanical energy to hydraulic energy.

Mechanical energy \rightarrow Hydraulic oil \rightarrow fluid power.

Classification of pump:-

- (1) positive displacement pump.
- (2) Rotary type (keto-dynamic) pump.

(1) positive displacement pump:-

→ Reciprocating pump.

(2) Rotary - tube

→ centrifugal pump.

or other specified pump like:-

(1) Vane pump.

(2) screw pump.

(3) Rotary pump.

(4) Jet pump.

(5) Gear pump (it is basically used in industrial sector).

→ it is two types:

(i) internal pump

(ii) External gear pump

GEAR PUMP:-

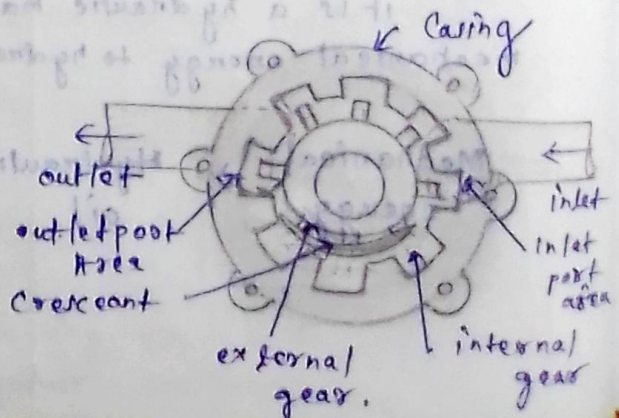
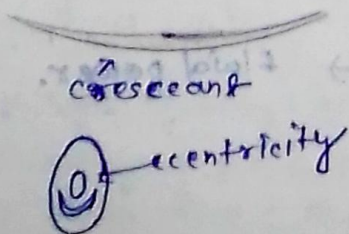
→ In this pump gear is used to generate power.

→ These pump is works on gear Arrangements one is internally & second is externally.

INTERNAL GEAR PUMP

→ These pump is work on internally gear arrangement.

→ spur gear is used.



EXTERNAL GEAR PUMP :-

- These pump is work on external gear arrangement.
- spur gear is used.

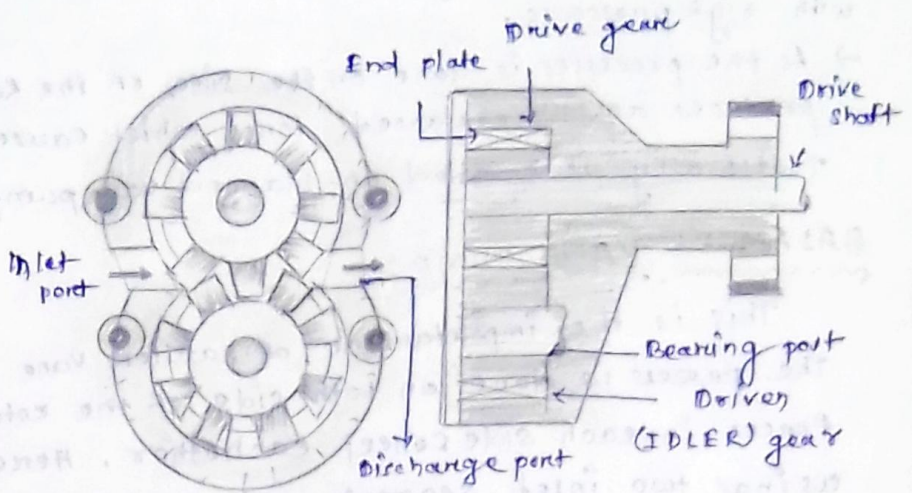


Fig:- External Spur gear pump;

VANE PUMP :-

This pump is also widely used in the hydraulic control system which consists of vanes cut into the rotor to produce power. These pump can be divided into two types:-

(1) Balanced vane pump.

(2) Unbalance vane pump.

(1) UNBALANCED VANE PUMP :-

→ Here also power produced due to centrifugal action.

→ it consists of Rotor, Vanes, Cam ring etc.

→ Initially due to pressure difference oil is trapped into the rotor.

→ Vane is connected in cam ring (vane is move inward or outward).

→ it has two process

(1) suction.

(2) delivery.

→ Rotor - one side - force act. (to create vibration).

(1) SUCTION :-

when in starting the rotor is rotates in the shaft bearing and the vanes moves out ward causing pressure difference and let the fluid in (during 1st half of rotation).

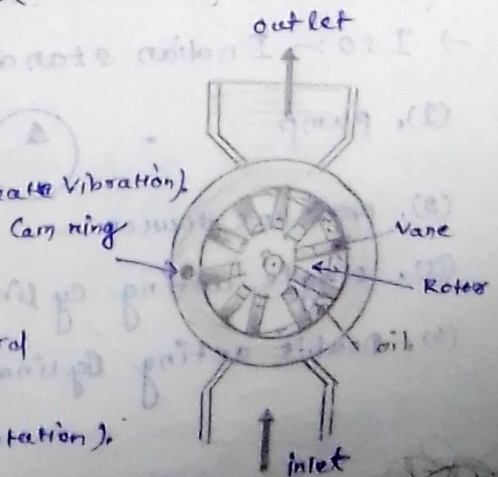


Fig:- simple vane pump

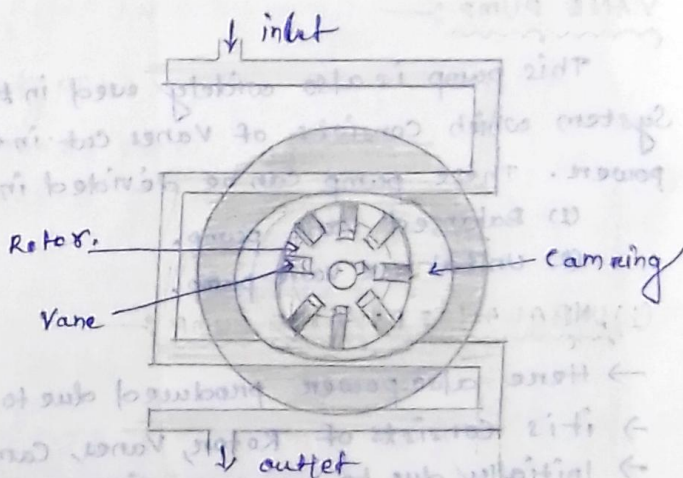
(3) Delivery? -

During the 2nd half rotation of the Rotor the Vanes moves inward causing a large force to eject that fluid with high pressure.

→ As the process is done on the side of the Rotor, it produces an un-balanced force which causes vibration. That's why it is called un-balanced vane pump.

BALANCED VANE PUMP:-

This is the improvement of earlier Vane pump here the process is done on both side of the rotor so that forces in each side cancel each other. Here we are using two inlet segments and outlet segments for better delivery.



"ISO" symbols of various hydraulic components:-







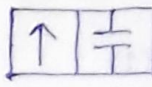
→ ISO: Indian standard organization,

(1). pump -

(2). pressure source -

(3). single acting cylinder -

(4). Double acting cylinder -

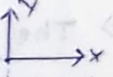

- (5). filter circuit - 
- (6). pressure gauge - 
- (7). Temperature gauge - 
- (8). Electric Motor - 
- (9). Cooler - 
- (10). Heater - 
- (11). 2-port 2 position Normally closed (DCV) - 

(port - connection of tuber in the circuit)
(T - Blocked path)

HYDRAULIC ACTUATORS :-

it is convert pressure energy (oil) to mechanical Energy.

Types of actuator :-

- 1. - linear - motion is transmitted in linear axis - 
- 2. - Rotary - motion is transmitted through rotation - 

1-linear cylinder :-

- (i) Telescopic cylinder.
- (ii) Tandem cylinder.

(R). Rotary Cylinder :-

- (i) screw motors, (ii) gear motors.

TELESCOPIC CYLINDER :-

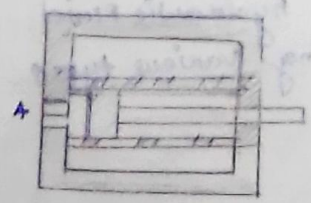


fig:- Retracted position.

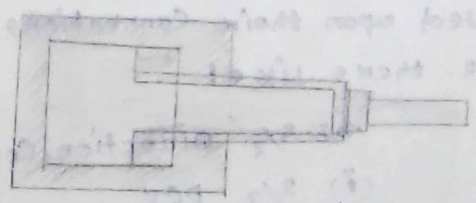


fig:- Extended position

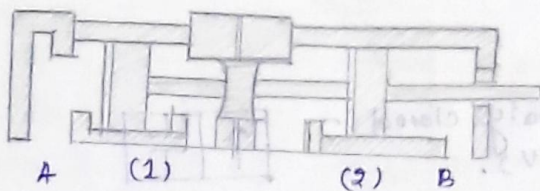
-> The piston rod for the first stage is used as piston Barrel for second stage.

→ it can be up to six stage.

→ it is used in hydraulic jacks, lifting, crans.

TANDEM CYLINDER ? (Tandam = 1+1)

This types of cylinder is used in medium level Application. here two or more cylinder connected in line so that when work is done by the cylinder gives two times stroke then normal operating cylinder.



→ it can be up to six stage cylinder.

PRESSURE CONTROL VALVE (PCV) ?

These valve are either hand operated, pilot, solenoid, spring operated valves.

→ The main fuction of these valve is to regulate the pressure in the hydraulic circuit,

used :-

(1). when the pressure in the circuit is more than the rated pressure.

(2). when there is reduction in pressure due to fluctuation in load.

(DCV) DIRECTION CONTROL VALVE ?

These are the most important valves. in hydraulic circuit as it controls the direction of hydraulic fluid Based upon their connections and working various types are there like!

(i) $3/2$ Direction Control valve.

(ii) $2/2$ DCV

(iii) $5/3$ DCV

(They may be operated by hand, spring solenoid, pilot valves)

Circuit Diagrams of DCV :-

- (1). 2/2 way Valve -
- (2). 2/3 way Valve -
- (3). 2/4 way Valve -

(4). 3/4 way DCV

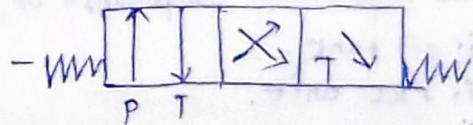
- (i) 1 p-point, 1 Temperature port
2, flow paths, 2 block paths



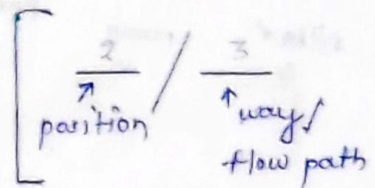
[if one block path
then]

(5). 3/4 way Valve

- 1 p-point, 1 Temperature port
1-block path, 3 flow paths,
spring return valve.



where,
(p = pressure port)
(T = Temperature port)



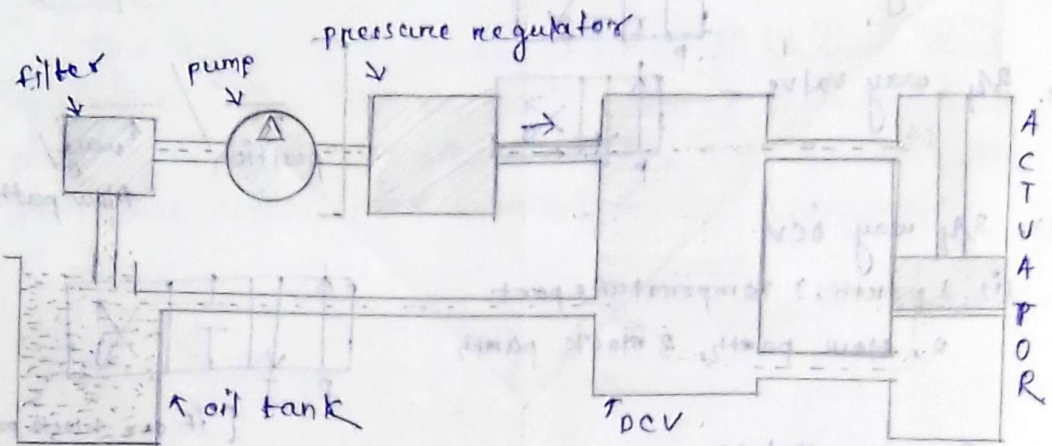
FLOW CONTROL VALVE :-

- The main function of the Flow Control Valves is to regulate the hydraulic fluid in the circuit.
- when we need to supply more fluid or less fluid according to the variable load condition.
 - when the excessive low pressure in the circuit in that condition, FCV is ^{immediately} stop/Brake the machine work.

Throttle Valve :-

Its working is same as used in case of governors, when the load on the circuit is low, it supplies less hydraulic fluid to the actuators whereas when the load in the circuit is very high, it supplies more hydraulic fluid to the actuators.

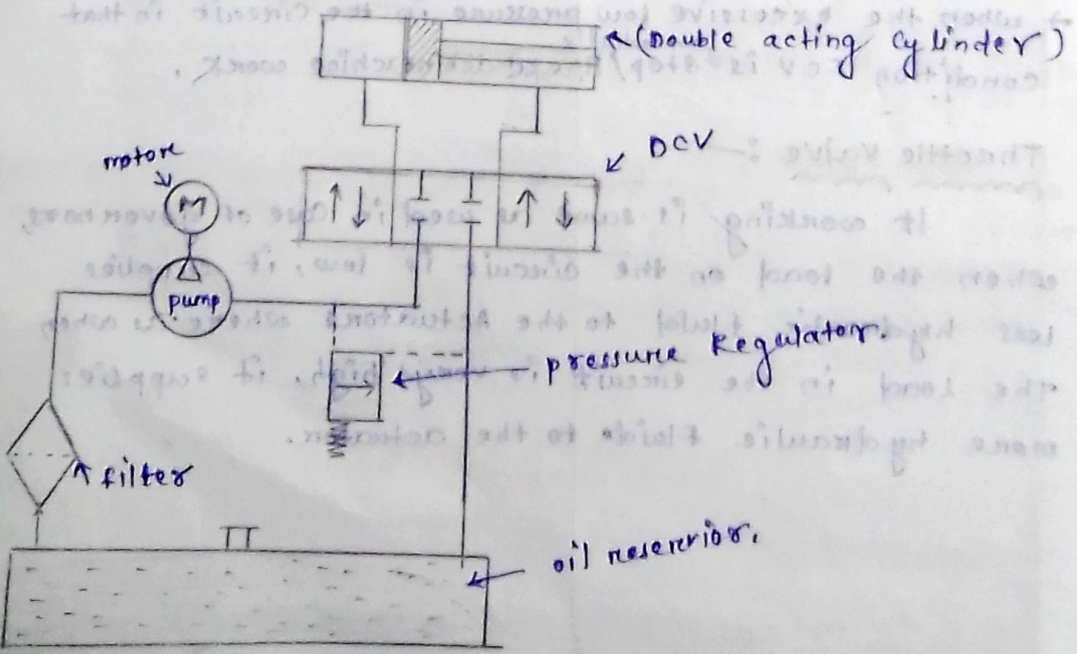
ESSENTIAL COMPONENTS OF HYDRAULIC CIRCUIT:



- * The important components of hydraulic control system are :-
- (i) oil tank.
 - (ii) FRL unit.
 - (iii) DCV.
 - (iv) pump.
 - (v) actuator.
 - (vi) pressure regulator.

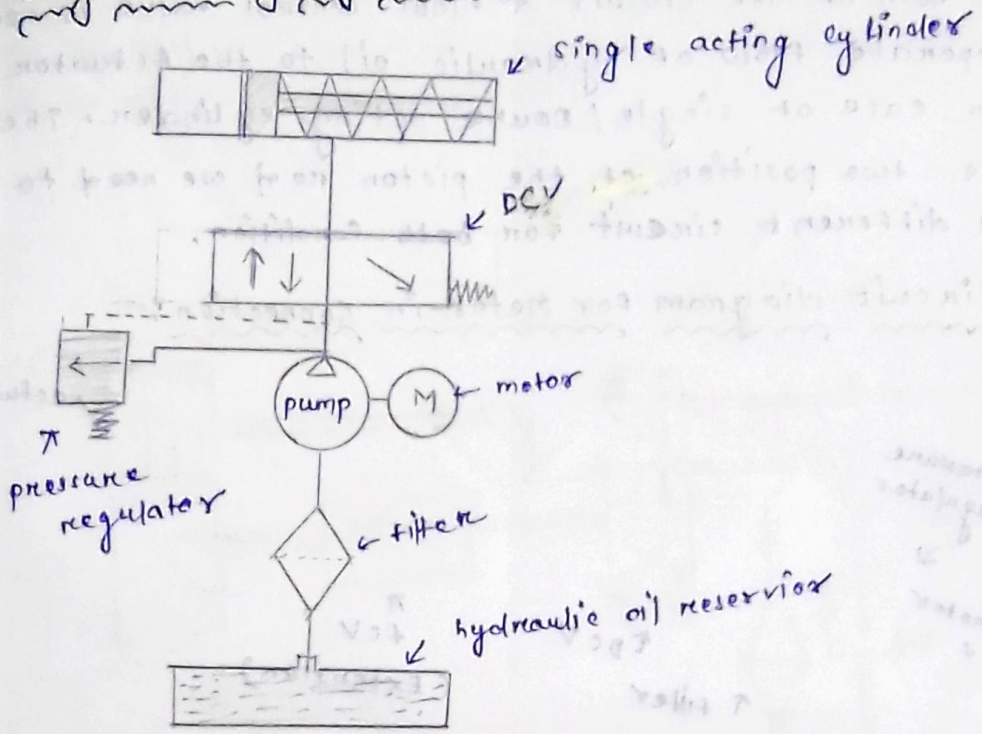
Direct control of Double acting cylinder in hydraulic:-

* Circuit diagram:-

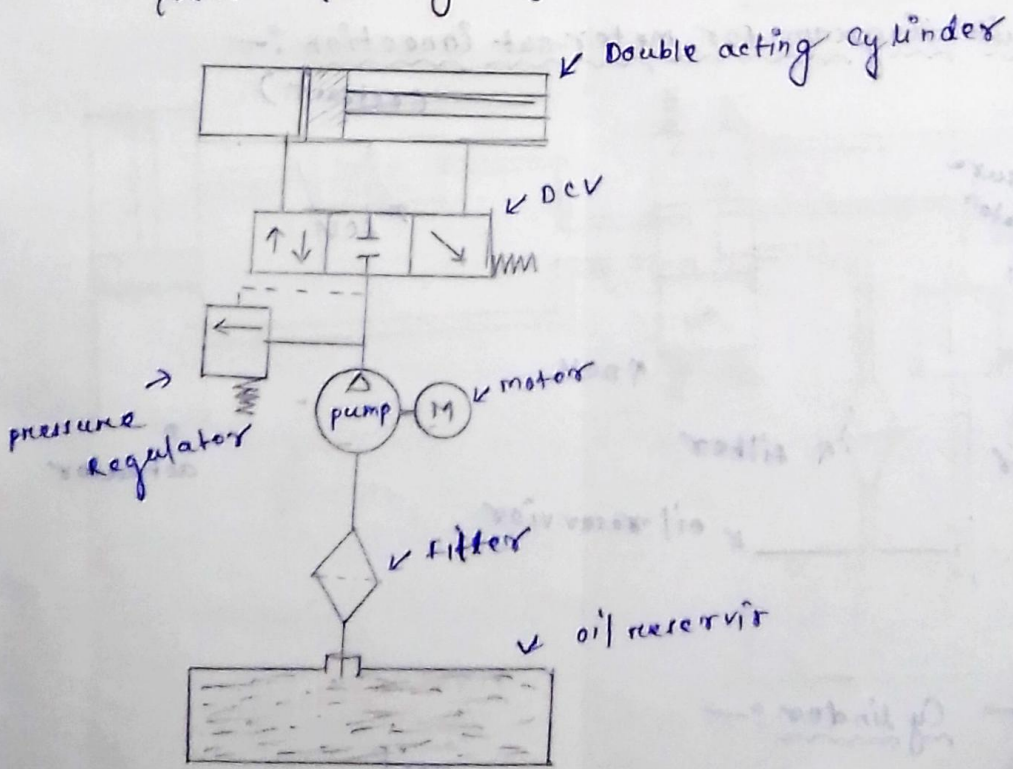


* Direct Control of single & Double acting Cylinder :-

(1) single acting cylinder :-



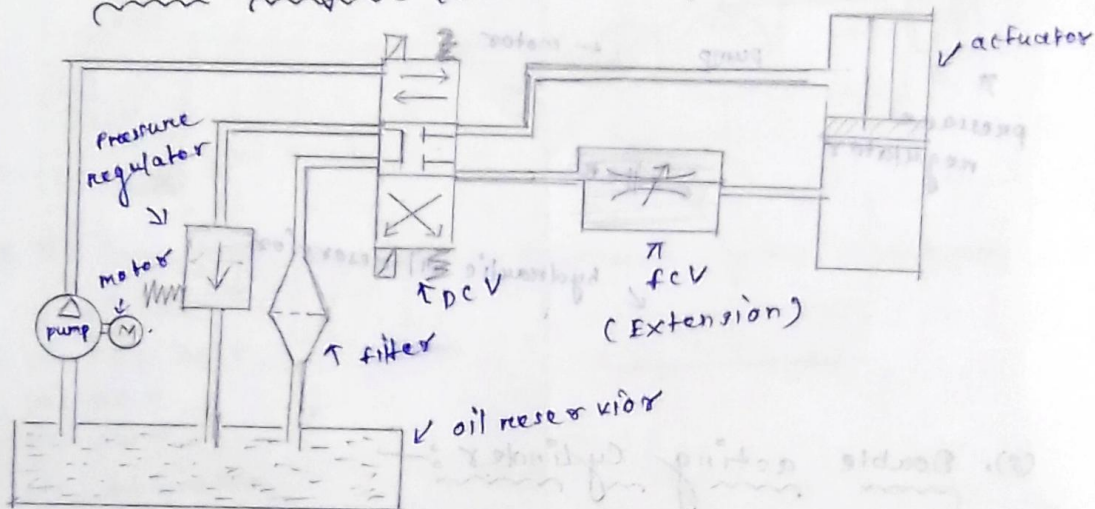
(2) Double acting cylinder :-



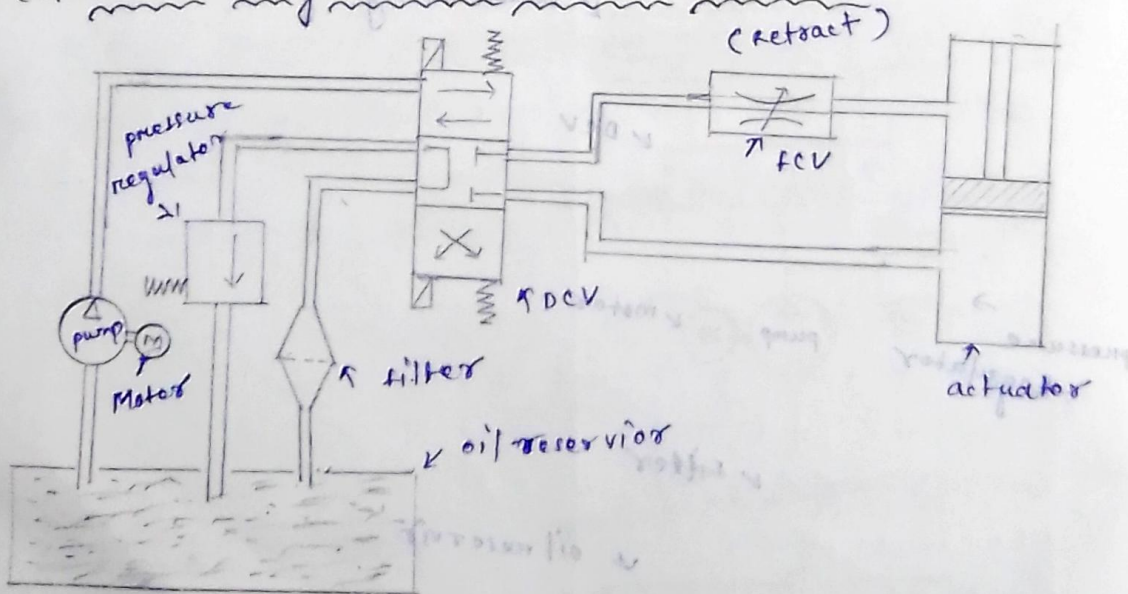
Meter-in & meter-out Connection in hydraulic Control system:-

In both of the circuit a Flow control valve is used to operate flow of hydraulic oil to the Actuator as in case of single / Double acting cylinder. There is the two position of the piston rod we need to draw different circuit for both condition.

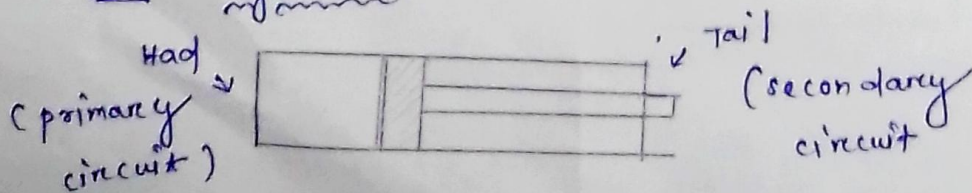
(1). Circuit diagram for meter-in connection:-



(2). Circuit diagram for meter-out connection:-



* MQ:- Cylinder:-



- * meter-in - flow is supplied before the load.
 - * meter-out - flow is supplied After the load.
- To control the speed of actuator is to used meter-in and meter-out connections.